

Organization of Knowledge and Taxation

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A classic question:

- How should people's incomes be taxed?

Renewed interest:

- Recent large changes in wage (and income) inequality.
- Wages change differently at the top and bottom.

Answer (to the classic question) typically given in models with:

- ① Exogeneous wage inequality, and/or
- ② limited interaction between top and bottom wages.

This paper:

- ① Optimal (labor) taxes in model with (i) endogeneous wages, (ii) rich interaction between top and bottom wages.
- ② Model can match the wage structure and (potentially) its changes over time.

- Model of knowledge based hierarchies of Garicano (2000), Garicano and Rossi-Hansberg (2006).
- People choose to become workers or managers.
- Form organizations in which knowledge efficiently combined.
- We extend the model to match observed wage inequality.
- Study labor income taxation in this model.

(Quantitative) Results

With a constant-rate-of-progressivity income tax function:

- More progressive taxes **decrease** wage inequality in upper tail: more managers supervise fewer (less diverse) workers.
- More progressive taxes **increase** wage inequality in lower tail: workers matched with more diverse managers.
- Nontrivial trade-off. However, in the optimum, taxes are:
 - ① **modestly more progressive** than in the U.S,
 - ② **much less progressive** than when wages are exogeneous.

Rest of the Talk

- Model
 - ① Environment
 - ② Competitive Equilibrium
 - ③ Comparative Statics
- Quantitative Analysis
 - ① Calibration
 - ② Optimal Taxes
- Empirical evidence
- Conclusion

Model

Setup

- Static model.
- Two goods: time and general consumption/output good.
- Government and measure one of agents: $U(c) - V(\ell)$.

$$U(c) = \ln c, \quad V(\ell) = \kappa \frac{\ell^{1+\eta}}{1+\eta}.$$

- Output produced by solving **tasks**.
- Agents heterogeneous in **skill** $z \in [\underline{z}, \bar{z}] \sim G(z)$.
- Every unit of time, continuum of tasks arrives $\sim F(z)$.
- Agent with skill z can solve $[\underline{z}, z]$ tasks.

Organizations

- Agents form **organizations** with one **manager** and n **production workers**.
- Worker of type z_p solves $F(z_p)$ tasks, and asks the manager for help with $1 - F(z_p)$ tasks.
- Manager of type $z_m > z_p$ explains $F(z_m) - F(z_p)$ tasks to worker.
- After receiving advice, worker produces output $F(z_m)$ per unit of time, and $F(z_m)\ell_p$ total (team) output.

- Communication between worker and manager takes time; number of workers n a manager working ℓ_m can supervise:

$$n\theta(z_p) = \ell_m$$

Example 1

(Garicano, 2000, constant communication costs h):

$$\theta(z_p) = h \cdot [1 - F(z_p)]$$

- **Example 2**

(this paper, heterogeneity in communication costs):

$$\theta(z_p) = h(z_p) \cdot [1 - F(z_p)], \quad h'(z_p) < 0.$$

- Output of organization is

$$nF(z_m)\ell_p = \frac{\ell_p}{\theta(z_p)} F(z_m)\ell_m$$

- Complementarity between i) skills, ii) hours worked
- Effective communication costs $\frac{\theta(z_p)}{\ell_p}$ critical

- Individuals sort to be production workers or managers.
- Production workers receive wage $w(z_p)$. Earnings

$$y_p = w(z_p)\ell_p$$

- Managers z_m teaming with n workers z_p have earnings

$$y_m = n [F(z_m) - w(z_p)] \ell_p = \frac{\ell_p}{\theta(z_p)} \cdot [F(z_m) - w(z_p)] \ell_m$$

with wages $w(z_m) = y_m/\ell_m$.

- Income taxed by a type-independent *constant-rate-of-progressivity* tax function:

$$T(y) = y - \lambda y^{1-\tau}$$

- Government consumption G , budget constraint

$$\mathbb{E}_y T(y) = G,$$

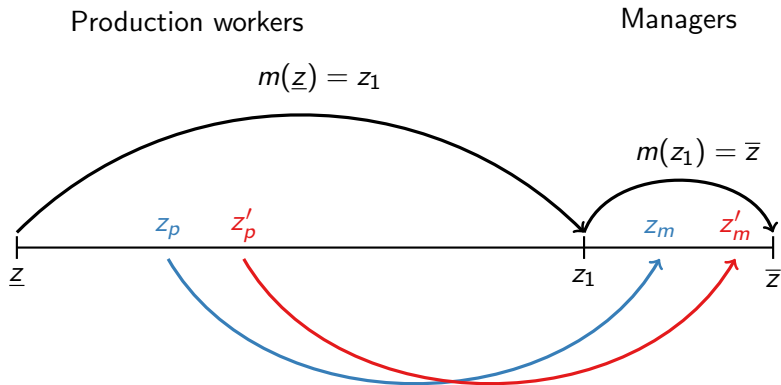
- Remark:** With this tax and utility functions, labor hours constant across agents; $\bar{\lambda}(\tau)$.

Equilibrium

CE is an allocation (assignment, labor hours and consumption) and prices (wages) s.t.:

- (a) Individuals optimally choose to be managers or workers.
- (b) Workers choose ℓ and c optimally given wages.
- (c) Managers choose workers and ℓ and c optimally, taking wage schedule and labor hours of production workers as given.
- (d) Supply of managers/workers equal to demand for managers/workers.
- (e) Supply of goods equal to demand for goods.

Occupational Choice



Assortative matching: $m'(z_p) > 0$

What happens when τ increases?

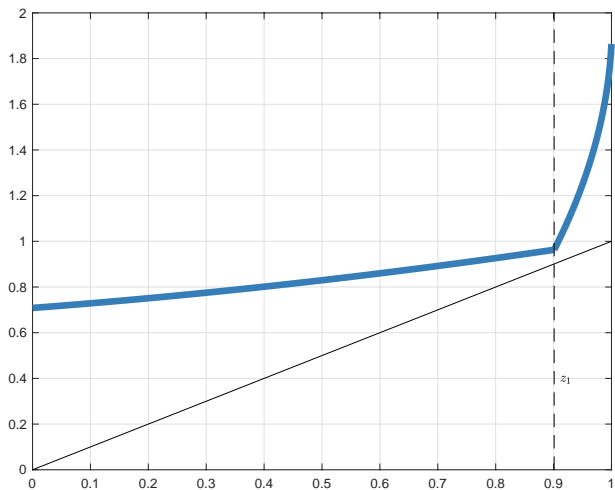
- Labor hours $\bar{\lambda}(\tau)$ decrease, effective com. costs $\frac{\theta(z_p)}{\ell_p}$ increase.
- Threshold z_1 decreases.
- Wage structure changes.

An Increase in Tax Progressivity

Consider a simple example with a closed form solution:

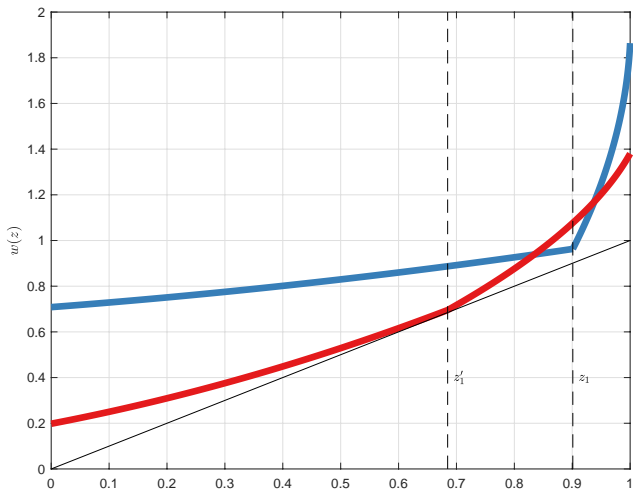
- $z \in [0, 1]$
- F and G are uniform
- $\theta(z_p) = h(1 - z_p)$
- The effective communication costs are $h/\bar{\ell}(\tau)$

Initial Equilibrium



Blue: Initial equilibrium wage structure.

Comparative Statics



Blue: Initial equilibrium wage structure. Red: z higher progressivity/a decrease in hours.

Comparative Statics

Tax progressivity $\tau \uparrow$ (effective communication cost \uparrow):

- ① Managers work less: More managers, smaller organizations.
- ② Wage inequality among managers decreases.
 - Intuition: Managers now matched with more similar workers.
 - Workers' hours decrease.
- ③ Wage inequality among workers increases.
 - Intuition: Workers matched with more diverse managers.

Summary: Endo wages affect the E-E tradeoff and make redistribution through progressive taxes less attractive.

Quantitative Analysis

- Calibrate model to U.S. wage moments.
- Compute optimal taxes (progressivity):
 - ① When wages are endogeneous.
 - ② When wages are exogeneous.
- Extensions/additional exercises.

Calibration: Functional Forms

- Skill types and tasks on $[0, 1]$.
- Skill types and task arrival:

$$G(x) = 1 - (1 - x)^{1+\rho}$$

$$F(x) = x$$

- **Note:** $F \sim U[0, 1]$ WLOG. Degree of freedom in G and F .
- $\theta(x) = h(1 - x)^\gamma [1 - F(x)] = h(1 - x)^{1+\gamma}$.

Calibration: Parameters

Parameters set outside the model

- Gvt policy

- ① $T(y) = y - \lambda y^{1-\tau}$, $\tau = 0.181$ (HSV, 2016),

- ② gvt expenditure $G = 0$.

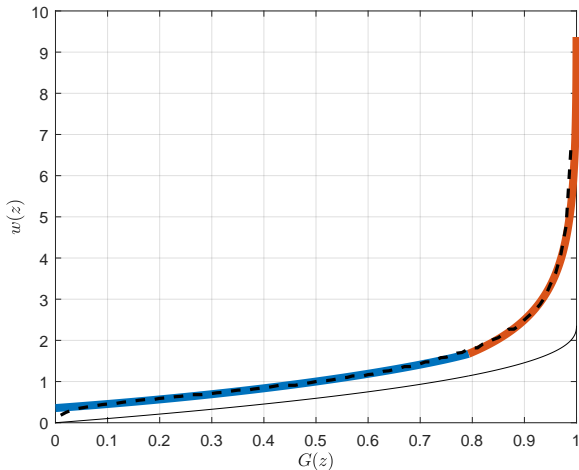
- Utility $\ln c - \kappa \frac{\ell^{1+\eta}}{1+\eta}$

- ① $\eta = 2$ (Frisch elasticity of labor = 0.5),

- ② normalize $\kappa = 1$.

- 3 remaining model parameters: ρ , γ and h .
- 3 targets:
 - ① $1 - G(z_1) = 0.207$ (fraction of managers, CPS 2017)
 - ② $\log 90/50 = 0.916$ (CPS 2017)
 - ③ $\log 50/10 = 0.788$ (CPS 2017)

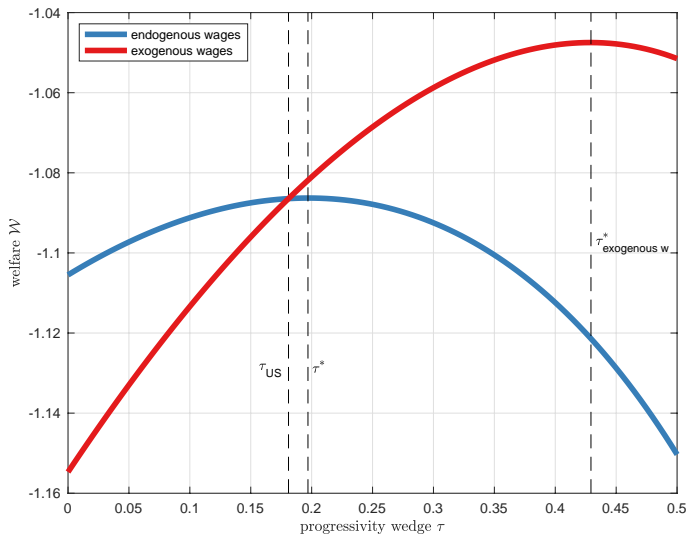
Benchmark Model Fit



Thick line: Model wages. Dashed line: CPS data. Thin line: 'Autarky'.

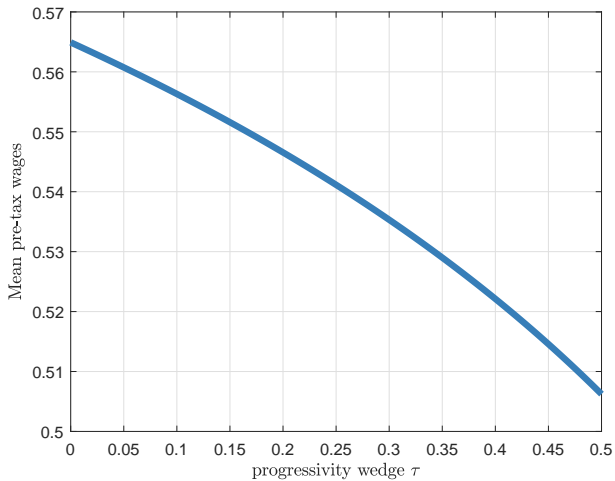
Optimal Taxes

Optimal Taxes

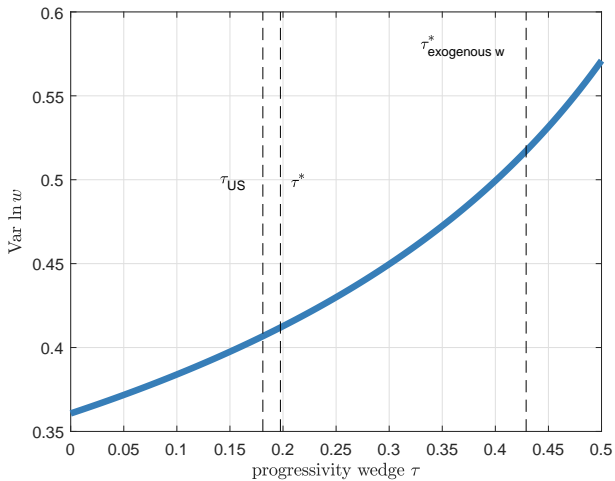


Red line: endogenous wages. Blue line: exogenous wages

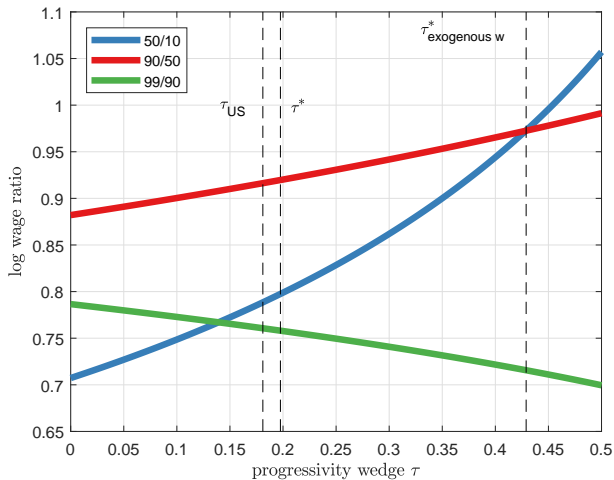
Mean Wages



Variance of log Wages



Wage Inequality Measures



Optimal Tax Reform

- $\tau_{US} = 0.181, \tau^* = 0.197, \tau_{exogenous\ w}^* = 0.429$.
- Welfare gains $\tau^* = 0.01\%, \tau_{exogenous\ w}^* = -3.45\%$.
- In addition to more redistribution and standard labor supply effects, higher progressivity:
 - ① \downarrow average pre-tax wages,
 - ② \downarrow wage inequality at top, but \uparrow wage inequality elsewhere (at bottom): \uparrow overall wage inequality.
- These effects \downarrow optimal tax progressivity from 0.429 to 0.197.

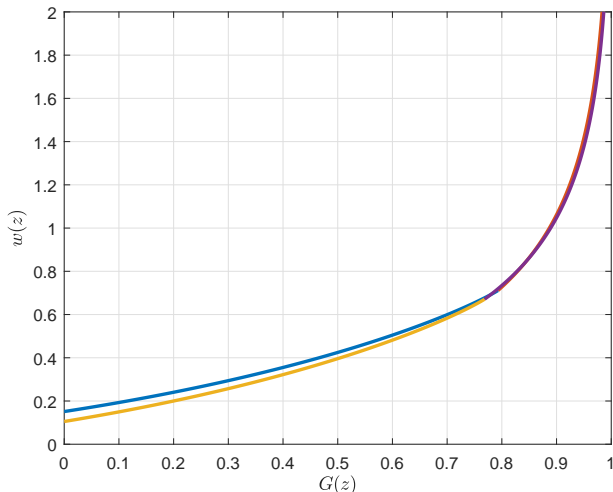
Distributional Consequences

Distributional Consequences

- Compare status-quo tax progressivity $\tau = 0.181$ with optimal exo-wage $\tau = 0.429$

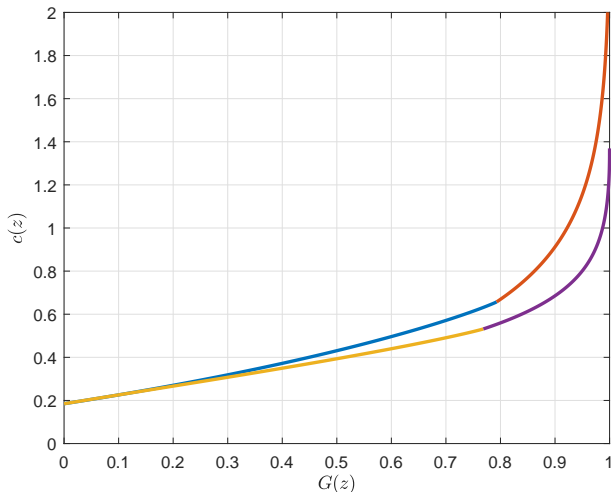
- Recall: optimal endo-wage $\tau = 0.197$.

Benchmark Additional Results - Wages



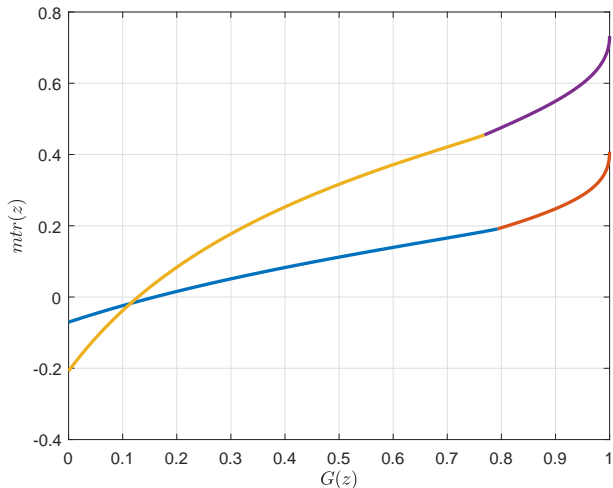
Blue+red: status quo $\tau = 0.181$, yellow+purple $\tau = 0.429$.

Benchmark Additional Results - Consumption



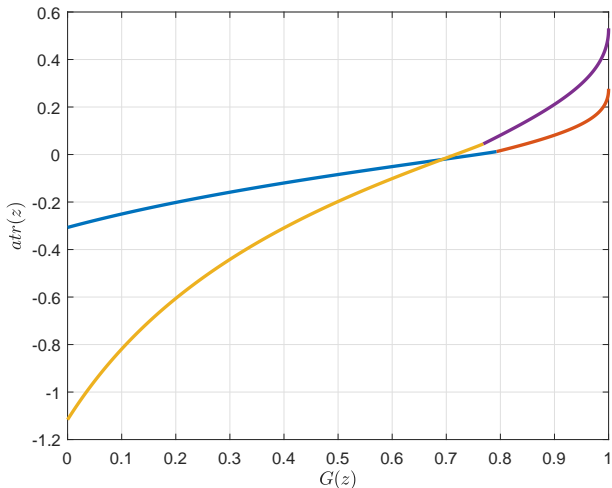
Blue+red: status quo $\tau = 0.181$, yellow+purple $\tau = 0.429$.

Benchmark Additional Results - Marginal Tax Rates



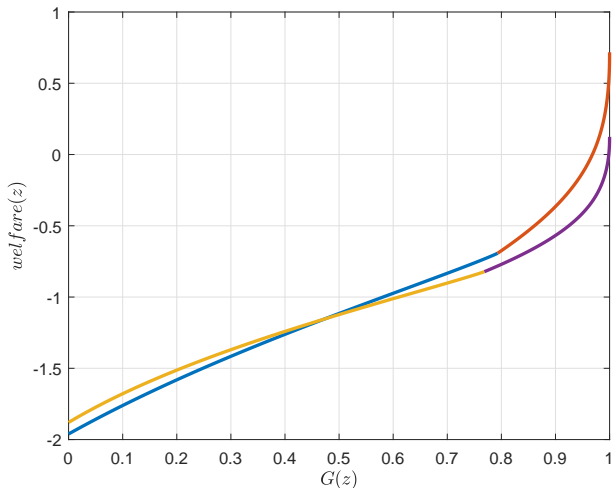
Blue+red: status quo $\tau = 0.181$, yellow+purple $\tau = 0.429$.

Benchmark Additional Results - Average Tax Rates



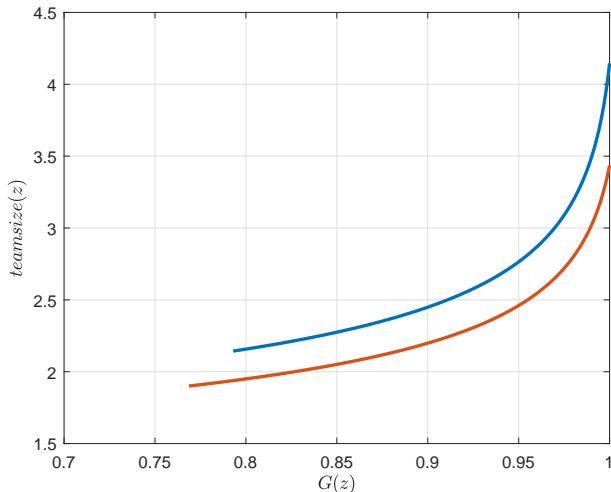
Blue+red: status quo $\tau = 0.181$, yellow+purple $\tau = 0.429$.

Benchmark Additional Results - Welfare



Blue+red: status quo $\tau = 0.181$, red $\tau = 0.429$.

Benchmark Additional Results - Teamsize



Blue+red: status quo $\tau = 0.181$, yellow+purple $\tau = 0.429$.

Empirical Evidence

Our mechanism: Progressivity affects pre-tax wages.

- Large empirical literature on how taxes affect labor supply and on how taxes affect pre-tax income.
- Smaller literature on how taxes affect pre-tax wages.
- Comparing our results to empirical literature work in progress.

Papers estimate wage responses to marginal tax rate (MTR) and average tax rate (ATR) changes:

- Scandinavian data (search-and-matching bargaining context):
 - ① Arronson et al (1997), Hansen et al (2000): increasing MTR decreases wages; opposite for ATR
 - ② Blomquist and Selin (2010): increasing MTR decreases wages for both men and women using Swedish data
 - ③ Holmlund and Kolm (1995): increasing progressivity leads to lower wages (and hence higher employment)

Our model predicts distributional consequences of changes in progressivity:

- Schneider (2005): German tax reforms, increasing progressivity reduces wages, stronger for lower income workers
- Frish, Zussman, Igdalov (2020): Israeli tax cuts, wage elasticity increases with income
- Moffitt, Wilhelm (1998): Wages of rich men have increased due to the 1986 U.S. tax rate cuts

Conclusion

- Model in which taxes interact with top/bottom wage inequality.
- Top/bottom inequality moves in opposite directions: more progressive taxes decrease top but increase bottom inequality.
- Optimal progressivity close to current U.S. tax code and substantially smaller relative to exogenous wages.