

Testing for Bubbles in Housing Markets: A Panel Data Approach

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Outline

Introduction

Bubbles in Housing Markets

Data

Panel Data Tests

Comparison with Other Housing Market Indicators

Summary

Introduction

Is There a Bubble?

- ▶ National data - Mc Carthy and Peach (2004), Galin (2004)
- ▶ Panel data - Malpezzi (1999), Galin (2006)
- ▶ Regional data - Smith and Smith (2006), Himmelberg, Mayer, Sinai (2005)

Stationarity and Earnings

- ▶ Campbell and Shiller (1987), Wang (2000)

Introduction

Panel Data Tests

- ▶ Cross section dependence - Pesaran (2004)
- ▶ Unit roots - Im, Pesaran, and Shin (2003), Pesaran (2007)
- ▶ Cointegration - Pedroni (1999, 2004)
- ▶ Causality - Hurlin (2004), Hurlin and Venet (2004)
- ▶ Application - Malpezzi (1999), Galin (2006)

Research Objective

- ▶ Combine panel data unit root and integration tests - bubble indicator
- ▶ US real estate market, house prices and rents
- ▶ Changes in house prices and rents

Present Value Model

House Prices and Cash Flows

$$P_{i,t} = E_t \left[\frac{C_{i,t+1} + P_{i,t+1}}{1 + D} \right], \quad i = 1, \dots, N$$

$$P_{i,t} = E_t \left[\frac{C_{i,t+1}}{1 + D} + \frac{C_{i,t+2}}{(1 + D)^2} + \dots + \frac{C_{i,t+k}}{(1 + D)^k} + \frac{P_{i,t+k}}{(1 + D)^k} \right]$$

$$\lim_{k \rightarrow \infty} E_t \left[\frac{P_{i,t+k}}{(1 + D)^k} \right] = 0$$

$$P_{i,t}^F = \sum_{j=1}^{\infty} \frac{1}{(1 + D)^j} E_t [C_{i,t+j}]$$

Present Value Model

Cash Flow Process I(1) and No Bubbles

$$\begin{aligned}S_{i,t} &= P_{i,t} - \frac{1}{D} C_{i,t} \\ &= \frac{1}{D} E_t \sum_{j=0}^{\infty} \frac{\Delta C_{i,t+j+1}}{(1+D)^j} \\ &= \frac{1}{D} E_t [\Delta P_{i,t+1}]\end{aligned}$$

Rational Bubbles

$$B_{i,t} = \frac{1}{1+D} E_t B_{i,t+1}$$

$$P_{i,t} = P_{i,t}^F + B_{i,t}$$

Present Value Model

Stationarity of house prices and cash-flows

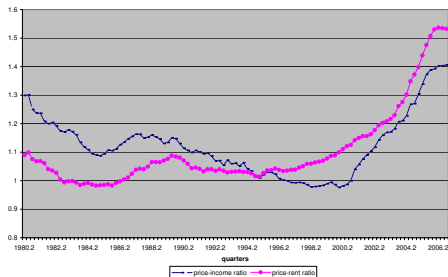
- ▶ Case 1: $P_{i,t}$ stationary and $C_{i,t}$ stationary
- ▶ Case 2: $P_{i,t}$ stationary and $C_{i,t}$ non-stationary
- ▶ Case 3: $P_{i,t}$ non-stationary and $C_{i,t}$ stationary
- ▶ Case 4: $P_{i,t}$ non-stationary and $C_{i,t}$ non-stationary

Bubble Indicator

- ▶ $=0$ in Case 1, 2
- ▶ $=1$ in Case 3
- ▶ $=p$ value of a stationarity test of P/r in Case 4

Aggregate Data

Aggregate Price-Income and Price-Rent Ratios



Panel Data

Dataset 1 - 23 Metropolitan Statistical Areas (MSA), 1978:1-2006:2

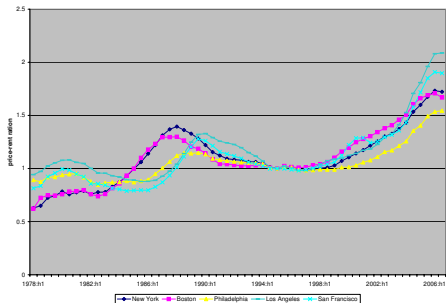
- ▶ House price index (HPI) from the Office of Federal Housing Enterprise Oversight (OFHEO) - the weighted repeat sales index based on mortgage contracts
- ▶ Rent of primary residence index (RI) estimated by the Bureau of Labor Statistic (BLS)
- ▶ Regional CPI from (BLS)

Dataset 2 - 273 Metropolitan Statistical Areas, 1986-2006

- ▶ HPI from OFHEO
- ▶ The fair market rent, US Department of Housing and Urban Development (HUD)
- ▶ Aggregate CPI from BLS

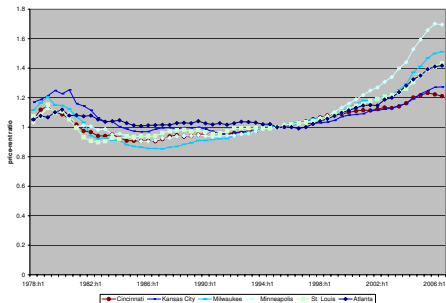
Panel Data

Price-Rent Ratios in 23 MSA



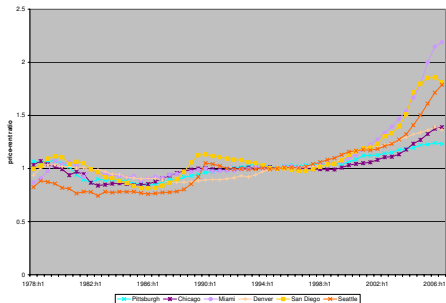
Panel Data

Price-Rent Ratios in 23 MSA



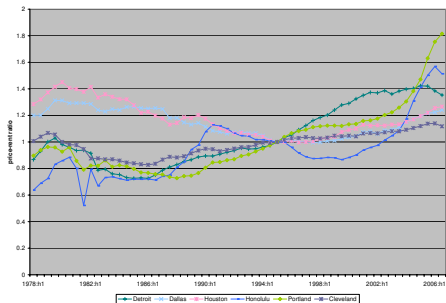
Panel Data

Price-Rent Ratios in 23 MSA



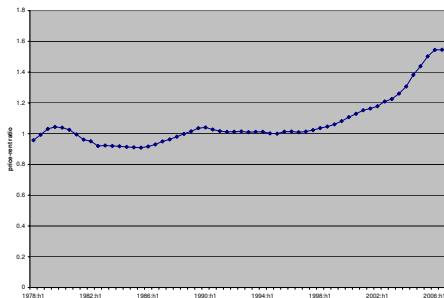
Panel Data

Price-Rent Ratios in 23 MSA



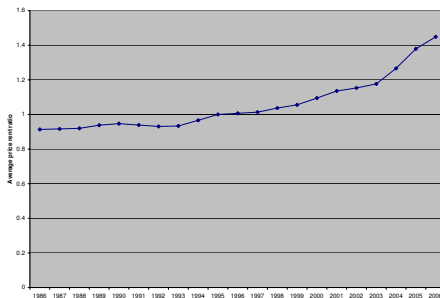
Panel Data

Average Price-Rent Ratios in 23 MSA



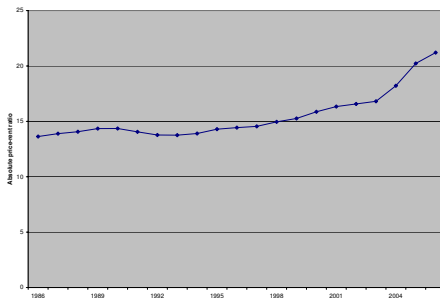
Panel Data

Average Price-Rent Ratios in 273 MSA



Panel Data

Average Absolute Price-Rent Ratios in 273 MSA



Panel Data

Price-rent Ratios Using Indices, 273 MSA's

| | $P/r > 1.5$ | $P/r > 1.3$ | $P/r < 0.9$ | $P/r < 0.8$ |
|------|-------------|-------------|-------------|-------------|
| 1986 | 2 | 11 | 142 | 76 |
| 1987 | 5 | 15 | 145 | 72 |
| 1988 | 7 | 20 | 141 | 76 |
| 1989 | 3 | 18 | 130 | 72 |
| 1990 | 2 | 16 | 119 | 60 |
| 1991 | 1 | 5 | 116 | 50 |
| 1992 | 0 | 1 | 116 | 47 |
| 1993 | 0 | 0 | 105 | 36 |
| 1994 | 0 | 0 | 5 | 0 |
| 1995 | 0 | 0 | 0 | 0 |
| 1996 | 0 | 0 | 1 | 0 |
| 1997 | 0 | 0 | 1 | 0 |
| 1998 | 0 | 0 | 2 | 0 |
| 1999 | 0 | 5 | 4 | 0 |
| 2000 | 2 | 14 | 1 | 0 |
| 2001 | 7 | 28 | 3 | 0 |
| 2002 | 10 | 39 | 3 | 0 |
| 2003 | 16 | 54 | 4 | 0 |
| 2004 | 42 | 84 | 3 | 0 |
| 2005 | 74 | 118 | 2 | 0 |
| 2006 | 97 | 137 | 3 | 1 |

Panel Data

Price-rent Ratios Using Levels, 273 MSA's

| | P/r>22.5 | P/r>20 | P/r<13 | P/r<12 |
|------|----------|--------|--------|--------|
| 1986 | 10 | 13 | 70 | 64 |
| 1987 | 11 | 17 | 72 | 65 |
| 1988 | 12 | 19 | 71 | 64 |
| 1989 | 11 | 20 | 70 | 64 |
| 1990 | 13 | 18 | 70 | 63 |
| 1991 | 12 | 14 | 71 | 63 |
| 1992 | 10 | 14 | 70 | 63 |
| 1993 | 11 | 12 | 68 | 61 |
| 1994 | 10 | 12 | 71 | 54 |
| 1995 | 10 | 14 | 67 | 47 |
| 1996 | 10 | 12 | 67 | 47 |
| 1997 | 10 | 13 | 65 | 48 |
| 1998 | 11 | 16 | 61 | 44 |
| 1999 | 12 | 18 | 58 | 41 |
| 2000 | 14 | 22 | 54 | 38 |
| 2001 | 18 | 23 | 47 | 32 |
| 2002 | 19 | 25 | 47 | 30 |
| 2003 | 21 | 26 | 44 | 28 |
| 2004 | 24 | 32 | 36 | 20 |
| 2005 | 33 | 48 | 32 | 23 |
| 2006 | 40 | 52 | 26 | 22 |

Panel Data Tests

Pesaran (2004): Diagnostic tests for cross section dependence in panels

$$CD = \sqrt{\frac{2T}{N(N-1)}} \left(\sum_{i=1}^{N-1} \sum_{j=i+1}^N \text{Corr}(\hat{\epsilon}_i, \hat{\epsilon}_j) \right) \Rightarrow N(0, 1)$$

| | price-level <i>CD</i> | | price-diff. <i>CD</i> | | rent-level <i>CD</i> | | rent-diff. <i>CD</i> |
|--|--------------------------|-----|--------------------------|-----|-------------------------|-----|-------------------------|
| 23 MSAs, 1978:01-2006:02, semi-annual data | | | | | | | |
| | 75.12 | *** | 15.44 | *** | 29.13 | *** | 0.09 |
| 273 MSA, 1986-2006, annual data | | | | | | | |
| | 566.00 | *** | -2.58 | *** | 209.01 | *** | 0.63 |

Stationarity

Panel Data Unit Root Tests - Pesaran (2007)

- ▶ Cross-sectionally Augmented Dickey Fuller (CADF):

$$\Delta y_{it} = \mu_i + \omega_i t + \alpha_i y_{i,t-1} + v_i \bar{y}_{t-1} + \sum_{j=1}^{p_i} \lambda_{ij} \Delta y_{i,t-j} + \sum_{j=0}^{p_i} \varpi_{ij} \Delta \bar{y}_{i,t-j} + \varepsilon_{it}$$

- ▶ $H_0 : \alpha_i = 0$

$$H_1 : \begin{cases} \alpha_i = 0 & \text{for } i = 1, 2, \dots, N_1 \\ \alpha_i < 0 & \text{for } i = N_1 + 1, N_1 + 2, \dots, N. \end{cases}$$

- ▶ CADF: $\tilde{t}_{i,T_i,N}(p_i) = \tilde{t}_i(T, N)$

- ▶ CIPS: $\bar{t}^\dagger = \frac{1}{N} \sum_{i=1}^N \tilde{t}_i(N, T)$

CADF, 23 MSA

| MSA | price CADF | rent CADF | p/r CADF | p/r rank |
|---|---------------|--------------|-------------|-------------|
| Atlanta-Sandy Springs-Marietta, GA | -0.37 | -0.41 | -1.15 | 7 |
| Boston-Quincy, MA (MSAD) | -1.90 | -3.21 | -1.69 | 8 |
| Chicago-Naperville-Joliet, IL (MSAD) | -6.42 *** | -6.42 *** | -4.42 ** | 23 |
| Cincinnati-Middletown, OH-KY-IN | -4.73 *** | -1.32 | -2.75 | 19 |
| Cleveland-Arkon, OH (MSAD) | -4.73 *** | -4.53 *** | -2.23 | 12 |
| Dallas-Plano-Irving, TX (MSAD) | -2.95 | -1.68 | -2.93 | 21 |
| Denver-Aurora, CO | 0.89 | -0.12 | -0.78 | 5 |
| Detroit-Livonia-Dearborn, MI (MSAD) | -1.08 | -3.03 | -0.72 | 3 |
| Honolulu, HI | -0.13 | -0.79 | -0.49 | 2 |
| Houston-Sugar Land-Baytown, TX | -3.05 | -5.18 *** | -2.52 | 17 |
| Kansas City, MO-KS | -0.01 | -2.50 | -0.76 | 4 |
| Los Angeles-Long Beach-Glendale, CA (MSAD) | -1.78 | -1.79 | -2.5 | 16 |
| Miami-Miami Beach-Kendall, FL (MSAD) | -0.45 | -0.03 | -0.91 | 6 |
| Milwaukee-Waukesha-West Allis, WI | -4.40 ** | -2.36 | -2.33 | 15 |
| Minneapolis-St. Paul-Bloomington, MN-WI | 0.65 | -5.06 *** | -0.42 | 1 |
| New York-White Plains-Wayne, NY-NJ (MSAD) | -3.39 | -3.90 ** | -2.82 | 20 |
| Philadelphia, PA (MSAD) | -1.50 | -1.70 | -1.87 | 9 |
| Pittsburgh, PA | -3.32 | -2.76 | -2.27 | 13 |
| Portland-Vancouver-Beaverton, OR-WA | -2.08 | -2.29 | -1.89 | 10 |
| San Diego-Carlsbad-San Marcos, CA | -2.34 | -3.18 | -2.63 | 18 |
| San Francisco-San Mateo-Redwood City, CA (MSAD) | -2.80 | -2.00 | -2.28 | 14 |
| Seattle-Bellevue-Everett, WA (MSAD) | -2.96 | -2.95 | -3.51 * | 22 |
| St. Louis, MO-IL | -3.04 | -2.08 | -2.17 | 11 |

CADF, 273 MSA, Top 25

| MSA | price CADF | rent CADF | p/r CADF | p/r rank |
|--|---------------|--------------|-------------|-------------|
| Ann Arbor, MI | -0.82 | -1.37 | 0.20 | 8 |
| Athens-Clarke County, GA | 1.48 | -1.44 | -0.11 | 12 |
| Barnstable Town, MA | 1.44 | -1.71 | 1.70 | 1 |
| Bend, OR | -0.11 | -1.56 | 0.53 | 3 |
| Bridgeport-Stamford-Norwalk, CT | -0.06 | -1.51 | -0.56 | 19 |
| Canton-Massillon, OH | -1.46 | -2.20 | -0.46 | 17 |
| Deltona-Daytona Beach-Ormond Beach, FL | 1.16 | -1.46 | -0.59 | 20 |
| Des Moines-West Des Moines, IA | -2.68 | 0.39 | 0.08 | 9 |
| El Paso, TX | -2.10 | -3.34 | -0.52 | 18 |
| Flint, MI | -0.60 | -2.11 | -0.59 | 21 |
| Jackson, MI | 0.72 | -3.15 | 0.00 | 10 |
| Lakeland, FL | 0.17 | -1.52 | 0.52 | 4 |
| Las Vegas-Paradise, NV | -0.96 | -2.89 | 0.23 | 7 |
| Lexington-Fayette, KY | -1.15 | -2.18 | 0.47 | 5 |
| Mansfield, OH | -0.90 | -2.17 | -0.64 | 23 |
| Monroe, LA | -4.84 ** | -1.50 | -0.32 | 14 |
| New Haven-Milford, CT | -1.54 | -1.68 | -0.70 | 25 |
| Olympia, WA | -0.19 | -1.29 | -0.32 | 15 |
| Poughkeepsie-Newburgh-Middletown, NY | -0.50 | -1.36 | -0.06 | 11 |
| Rochester, MN | -1.28 | 0.98 | -0.27 | 13 |
| Saginaw-Saginaw Township North, MI | 0.34 | -3.01 | 1.02 | 2 |
| Sherman-Denison, TX | -2.81 | -1.31 | -0.68 | 24 |
| Spokane, WA | -0.63 | -1.00 | -0.61 | 22 |
| St. Joseph, MO-KS | -1.42 | -2.42 | -0.43 | 16 |
| Toledo, OH | 0.63 | -2.17 | 0.29 | 6 |

CADF, 273 MSA, Bottom 25

| | price | rent | p/r | p/r |
|--|-----------|-------|-----------|-----|
| Abilene, TX | -6.42 *** | -2.13 | -4.84 ** | 271 |
| Amarillo, TX | -6.34 *** | -0.18 | -4.42 ** | 268 |
| Atlantic City, NJ | -5.26 ** | -2.28 | -3.60 | 255 |
| Beaumont-Port Arthur, TX | -3.62 | -2.20 | -3.99 * | 262 |
| Boulder, CO | -2.97 | -1.80 | -4.53 ** | 269 |
| Burlington-South Burlington, VT | -5.79 *** | -1.97 | -3.83 * | 259 |
| Colorado Springs, CO | -4.27 ** | -1.66 | -3.47 | 249 |
| Corpus Christi, TX | -6.07 *** | -1.45 | -3.74 * | 256 |
| Dayton, OH | -3.77 * | -3.17 | -3.47 | 250 |
| Fort Lauderdale-Pompano Beach-Deerfield Beach, FL (M | 0.53 | -1.56 | -3.58 | 253 |
| Greeley, CO | -3.51 | 0.19 | -3.97 * | 261 |
| Houma-Bayou Cane-Thibodaux, LA | -5.97 *** | -2.22 | -3.56 | 252 |
| Knoxville, TN | -2.87 | -2.07 | -3.91 * | 260 |
| Los Angeles-Long Beach-Glendale, CA (MSAD) | -6.42 *** | -0.82 | -3.55 | 251 |
| Madison, WI | -2.89 | -3.02 | -4.77 ** | 270 |
| Ocean City, NJ | -3.90 * | -2.43 | -4.10 * | 264 |
| Oxnard-Thousand Oaks-Ventura, CA | -5.95 *** | -2.74 | -4.10 * | 265 |
| Philadelphia, PA (MSAD) | -4.93 ** | -1.56 | -6.42 *** | 273 |
| Phoenix-Mesa-Scottsdale, AZ | -3.50 | -1.84 | -4.02 * | 263 |
| Reading, PA | -6.17 *** | -1.42 | -4.20 ** | 267 |
| San Diego-Carlsbad-San Marcos, CA | -3.84 * | -1.03 | -3.80 * | 258 |
| Santa Cruz-Watsonville, CA | -3.88 * | -2.33 | -4.11 * | 266 |
| Scranton-Wilkes-Barre, PA | -3.21 | -0.28 | -5.49 *** | 272 |
| Shreveport-Bossier City, LA | -6.42 *** | -1.31 | -3.78 * | 257 |
| Waterloo-Cedar Falls, IA | -1.91 | -2.66 | -3.58 | 254 |

Panel Data Tests

Unit Roots Tests

23 MSA, 1978:01-2006:02, semi-annual data

| Method | price-level | price-diff. | | rent-level | rent-diff. | | p/r |
|--------|-------------|-------------|-----|------------|------------|-----|-------|
| IPS | 1.63 | -20.29 | *** | -2.60 | -13.00 | *** | 5.48 |
| CIPS | -2.26 | -5.02 | *** | -2.58 | -4.16 | *** | -2.00 |

273 MSAs, 1986-2006, annual data

| Method | price-level | price-diff. | | rent-level | rent-diff. | | p/r |
|--------|-------------|-------------|-----|------------|------------|-----|-------|
| IPS | 6.17 | -19.23 | *** | 5.84 | -22.16 | *** | 12.69 |
| CIPS | -2.35 | -2.74 | *** | -1.90 | -3.00 | *** | -2.12 |

Panel Data Tests

Pedroni (1999,2004) Cointegration Tests

- ▶ $y_{i,t} = \mu_i + \omega_i t + \psi_i x_{i,t} + \zeta_{i,t}$ for $t = 1, \dots, T$, $i = 1, \dots, N$.
- ▶ The null hypothesis of no cointegration: $H_0 : \gamma_i = 1$ for all i where γ_i is the autoregressive coefficient of the residual $\hat{\zeta}_i$
- ▶ The alternative hypothesis $H_1 : \gamma_i < 1$ for all i i.e. no common value for the autoregressive coefficient is presumed
- ▶ The critical values were generated using 50,000 simulations by bootstrapping to preserve cross-sectional dependence and including autocorrelation.

| Stat. | 23 MSA | 273 MSA |
|----------------|--------|---------|
| group adf-stat | 1.82 | 28.69 |

Panel Data Tests

Panel Data Granger Causality - Hurlin (2004) and Hurlin and Venet (2004)

- ▶ Let y_i and x_j be two stationary variables.

$$y_{it} = \mu_i + \sum_{l=1}^L \varphi_i^{(l)} y_{i,t-l} + \sum_{l=1}^L \delta_i^{(l)} x_{i,j,t-l} + \xi_{it}$$

ξ_{it} are normally i.i.d. with zero mean and finite heterogeneous variances and $\xi_i = (\xi_{i1}, \dots, \xi_{iT})'$ are independently distributed across groups.

- ▶ Homogeneous Non Causality (HNC):

$$H_0 : \delta_i = 0, \quad \forall i = 1, \dots, N, \quad \delta_i = (\delta_i^{(1)}, \dots, \delta_i^{(L)})'$$

$$H_1 : \delta_i = 0, \quad \forall i = 1, \dots, N_1, \\ \delta_i \neq 0, \quad \forall i = N_1 + 1, \dots, N,$$

where $N_1 \in [0, N)$ is not known.

Panel Data Tests

- ▶ $W_{NT}^{HNC} = (1/N) \sum_{i=1}^N W_{iT}$ where W_{it} denotes the Wald statistic associated with the individual test of H_0 for each $i = 1, \dots, N$
- ▶ $Z_{NT}^{HNC} = \sqrt{\frac{N}{2 \times L} \times \frac{(T-2L-5)}{(T-L-3)}} \times \left[\frac{(T-2L-3)}{(T-2L-1)} W_{NT}^{HNC} - L \right]$
converges in distribution to $N(0, 1)$ as $N \rightarrow \infty$ for a fixed $T > 5 + 2L$

Panel Data Tests

Hurlin Tests for Homogeneous Non-Causality in Panel Data

| H_0 | Z_{NT}^{HNC} | P-value |
|-------|----------------|---------|
|-------|----------------|---------|

22 MSAs, 1978:01-2006:02, semi-annual data

| | | |
|---|-------|------|
| price-diff. does not Granger cause rent-diff. | -1.70 | 0.09 |
| rent-diff. does not Granger cause price-diff. | -1.57 | 0.12 |

243 MSAs, 1986-2006, annual data

| | | |
|---|-------|------|
| price-diff. does not Granger cause rent-diff. | -5.51 | 0.00 |
| rent-diff. does not Granger cause price-diff. | -5.74 | 0.00 |

Bubble Indicator, 23 MSA

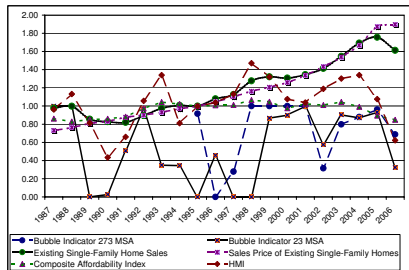
| Year | price CIPS | price-dif. CIPS | rent CIPS | rent-dif. CIPS | coint. Pedroni | p/r CIPS | bubble indicator |
|------|---------------|--------------------|--------------|-------------------|-------------------|-------------|---------------------|
| 1987 | -2.21 | | -2.71 * | | -1.32 | -2.62 | 1.00 |
| 1988 | -1.75 | -2.72 * | -2.65 * | -2.42 | 1.64 | -2.62 | 1.00 |
| 1989 | -2.71 * | -2.46 | -3.22 *** | -2.35 | 0.56 | -2.89 ** | 0.00 |
| 1990 | -2.41 | -2.67 * | -2.14 | -2.60 | 0.95 | -2.82 ** | 0.03 |
| 1991 | -1.51 | -2.75 ** | -1.89 | -2.56 | 0.66 | -2.18 | 0.51 |
| 1992 | -1.52 | -3.02 *** | -1.55 | -2.64 * | -3.11 | -1.63 | 0.97 |
| 1993 | -2.11 | -2.56 | -1.64 | -2.63 * | -2.68 | -2.31 | 0.35 |
| 1994 | -2.21 | -2.61 | -1.53 | -2.55 | -1.74 | -2.32 | 0.34 |
| 1995 | -2.71 * | -2.95 *** | -1.83 | -2.44 | -2.81 | -2.53 | 0.00 |
| 1996 | -2.23 | -2.55 | -1.83 | -2.51 | -2.05 | -2.22 | 0.46 |
| 1997 | -2.79 ** | -3.29 *** | -1.72 | -3.11 *** | -4.08 | -2.44 | 0.00 |
| 1998 | -2.96 *** | -3.15 *** | -2.08 | -3.15 *** | -6.44 *** | -2.70 * | 0.00 |
| 1999 | -1.91 | -3.07 *** | -2.25 | -2.79 ** | -2.35 | -1.85 | 0.87 |
| 2000 | -1.69 | -2.90 ** | -2.50 | -2.84 ** | -0.97 | -1.80 | 0.90 |
| 2001 | -2.07 | -3.59 *** | -2.66 * | -2.87 ** | 0.16 | -1.88 | 1.00 |
| 2002 | -1.83 | -3.48 *** | -1.89 | -2.51 | 0.39 | -2.13 | 0.58 |
| 2003 | -1.46 | -3.59 *** | -1.37 | -2.54 | 0.16 | -1.80 | 0.90 |
| 2004 | -1.58 | -3.23 *** | -0.81 | -2.41 | 0.69 | -1.85 | 0.87 |
| 2005 | -1.71 | -3.14 *** | -0.71 | -2.69 * | -0.81 | -1.75 | 0.93 |
| 2006 | -2.28 | -3.03 *** | -0.94 | -3.07 *** | -3.86 | -2.34 | 0.32 |

Bubble Indicator 273 MSA

| Year | price CIPS | price-dif. CIPS | rent CIPS | rent-dif. CIPS | coint. Pedroni | p/r CIPS | bubble indicator |
|------|---------------|--------------------|--------------|-------------------|-------------------|-------------|---------------------|
| 1995 | -2.03 | | -1.48 | | -18.05 | -1.88 | 0.92 |
| 1996 | -2.62 | -3.19 *** | -1.57 | -2.05 | -16.32 | -4.14 *** | 0.00 |
| 1997 | -2.39 | -3.09 ** | -2.35 | -1.93 | -14.06 | -2.54 | 0.28 |
| 1998 | -2.56 | -2.85 * | -2.31 | -2.73 | -2.86 | -0.85 | 1.00 |
| 1999 | -2.74 | -2.92 * | -3.33 *** | -2.67 | -3.85 | -1.18 | 1.00 |
| 2000 | -2.75 | -2.21 | -1.94 | -2.68 | -6.92 | -0.71 | 1.00 |
| 2001 | -2.75 | -2.28 | -3.39 *** | -2.97 ** | 4.88 | -2.74 | 1.00 |
| 2002 | -2.56 | -2.11 | -2.22 | -2.49 | 9.12 | -2.50 | 0.31 |
| 2003 | -1.42 | -2.05 | -2.21 | -2.29 | -0.46 | -2.04 | 0.80 |
| 2004 | -2.12 | -2.11 | -1.81 | -2.65 | -3.45 | -1.94 | 0.88 |
| 2005 | -2.40 | -1.95 | -1.40 | -2.16 | 7.11 | -1.78 | 0.96 |
| 2006 | -2.37 | -1.85 | -1.26 | -2.23 | 8.23 | -2.15 | 0.69 |

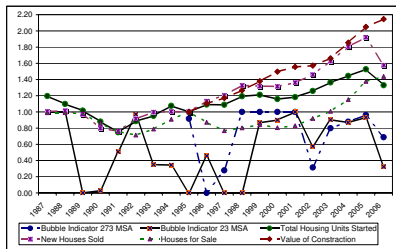
Comparison

Bubble and Other Indicators 1/2



Comparison

Bubble and Other Indicators 2/2



Summary

Panel Data - Stationarity

- ▶ Relationship between house prices and fundamentals is not stationary over the whole sample.

Bubble Indicators

- ▶ Rational bubbles in several periods but mainly in the late 1980s and the early 2000s up to 2005.
- ▶ Our bubble indicators coincide fairly well with the pattern of price-rent ratios, the HMI and the value of construction index.

Panel Data - Causality

- ▶ Changes in prices predict changes in rents and viceversa