

• INTRODUCING HOUSEHOLD ECONOMY

Bödel: "Not necessary change in preferences but a in the opportunity cost of time"

MODEL

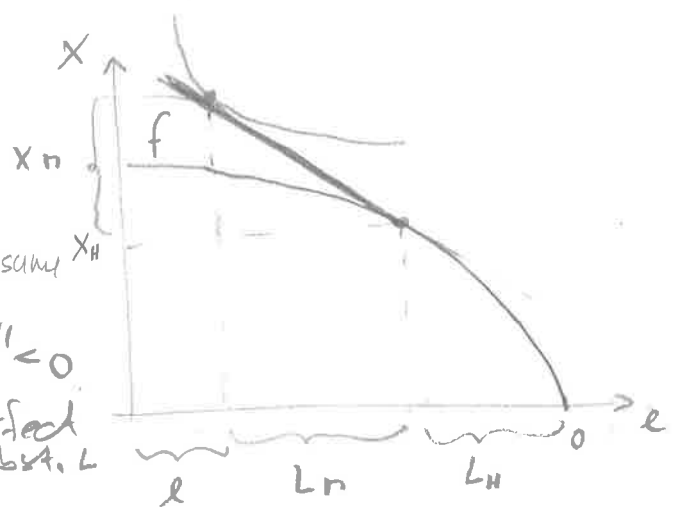
$$u = u(x, l)$$

$$x = x_H + x_n + x_o, p = 1$$

$$T = l + L_H + L_n \quad \rightarrow \frac{\partial f}{\partial x_n} = 0 \text{ assume } x_H$$

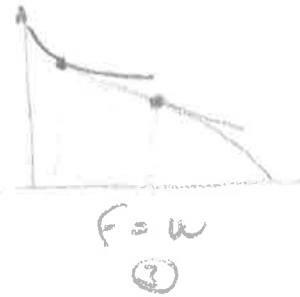
$$x_H = f(L_H) \quad ; \quad f' > 0, f'' < 0$$

$$x_H = \lambda + wL_n \quad ; \quad x_n \& x_H \text{ perfect subst. } L$$



What affects participation — on the L_n ?

$$f' \stackrel{?}{\gtrless} w$$



FONC in CASE ③

$$\frac{\partial u / \partial l}{\partial u / \partial x} = w = \frac{\partial f}{\partial L_n} = \frac{\partial u / \partial L_n}{\partial u / \partial x}$$

~~REQUIREMENTS~~

$$\mathcal{L}(x, l, \mu, \lambda) = u(x, l) + \lambda [x_o + wL_n + f(L_H) - x] + \mu [T - l - L_n - L_H]$$

$$\left. \begin{aligned} u_x - \lambda &= 0 \\ u_l - \mu &= 0 \end{aligned} \right\} \frac{u_l}{u_x} = \frac{\mu}{\lambda} = f' = w$$

$$\left. \begin{aligned} \lambda w - \mu &= 0 \\ \lambda f' - \mu &= 0 \end{aligned} \right\} \frac{w}{f'} = 1 \rightarrow w = f'$$

$$f' = \frac{\mu}{\lambda}$$

$u_x = -w > w$

You have 1 unit of time Δt to be used in three ways: l, l_H, l_M

leisure: $\Delta t \rightarrow \Delta l \rightarrow \Delta U^l = \frac{\partial U}{\partial l} \Delta t$ (i)

X home: $\Delta t \rightarrow \Delta l_H \rightarrow \Delta U^H = \frac{\partial U}{\partial x} \frac{\partial x}{\partial l_H} \Delta t$
 $= \frac{\partial U}{\partial x} f' \Delta t$ (ii)

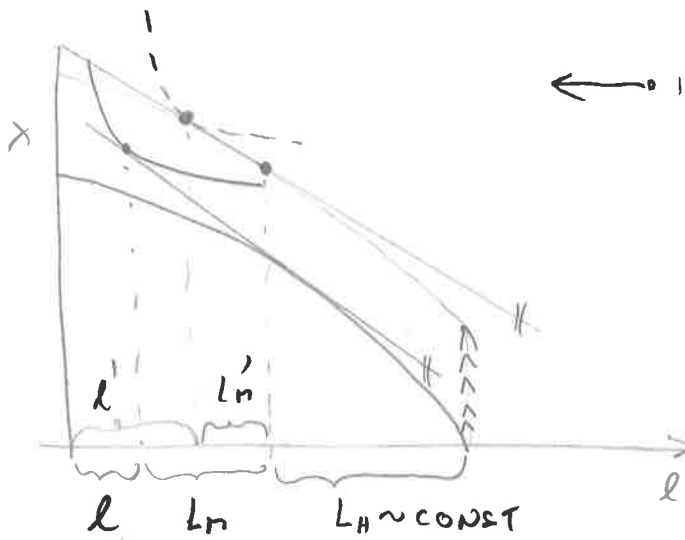
X work: $\Delta t \rightarrow \Delta l_M \rightarrow \Delta U^M = \frac{\partial U}{\partial x} w \frac{\Delta t}{(iii)}$

(i) & (ii): $\frac{\partial U}{\partial l} = f'$

(i) & (iii): $\frac{\partial U}{\partial l} = \text{MRS}_{l,x} = w$

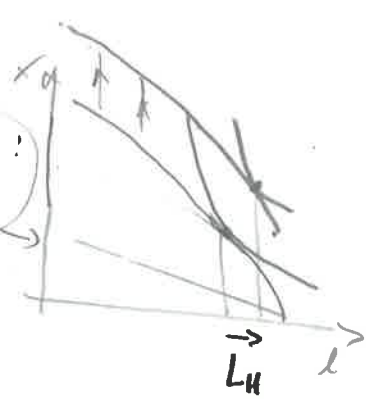
(ii) & (iii): $f' = w / p$

CASE Increase in non-labor income X_0

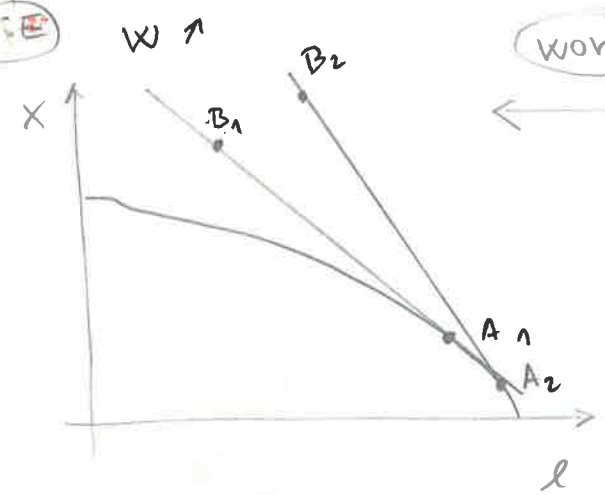


← if NORMAL GOOD, L_H will stay CONST.
 $\nearrow l'$
 $\searrow L_n$

IF not on the LM:
 $L_H \searrow, l \nearrow$

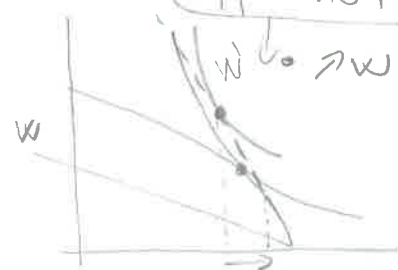


CASE



working person
 $L_H \searrow, L_n ?, l ?$

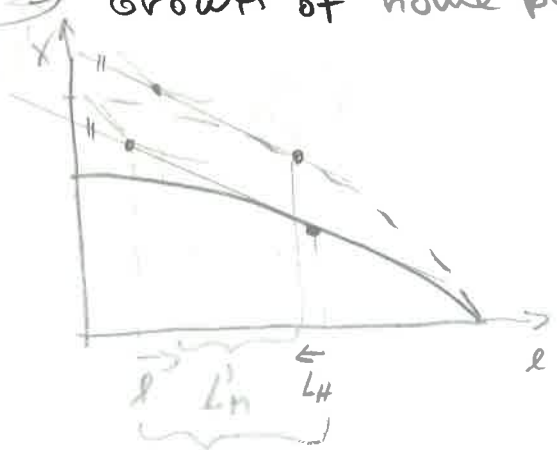
if not on the LM



$\nearrow w \Rightarrow$ no effect or participation
 $L_H \searrow, l ?, L_n ?$

CASE

Growth of home productivity (wage \nearrow , medicine, vacuum cleaner)



$L_H \nearrow, L_n \searrow, l \nearrow$

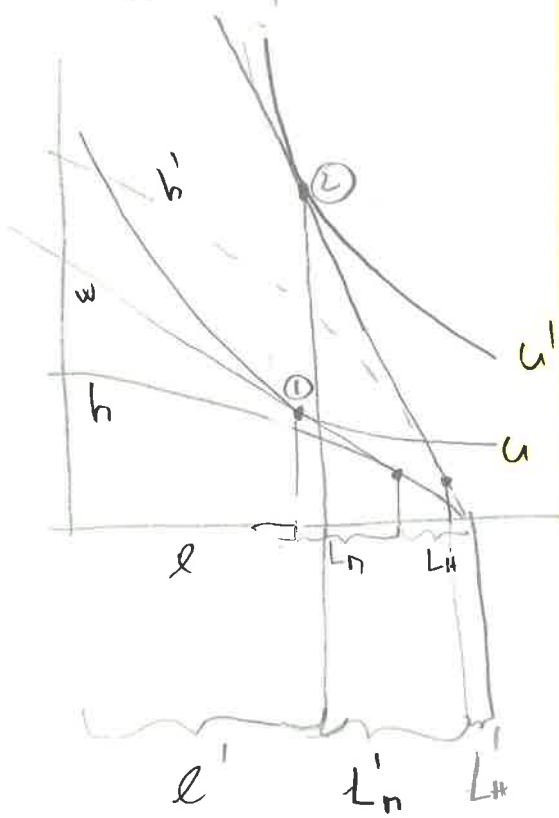
but empirically, we observe $L_H \searrow$
 why?

CASE

SCHOOLING - increases not only w but also shift $f(L_H) \nearrow$

CASE Change in home and market productivity during decades $\Delta x / \Delta L_M, \Delta x / L_H \uparrow$

① Change in $\Delta x / \Delta L_H$

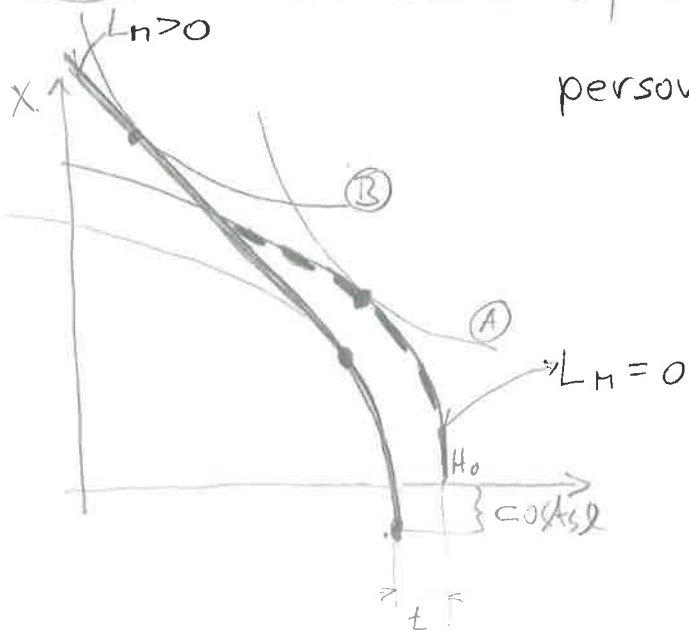


- $\Delta L_H \rightarrow$ if $\Delta w \uparrow \Rightarrow \Delta L \uparrow \Rightarrow \Delta L_H$
- ΔL_n & Δl depend on income & subst. eff.
- $l \rightarrow$ if subst. \gg income eff. $\hookrightarrow L_n \uparrow \uparrow$
- $l \rightarrow$ if subst. $<$ income eff. $\hookrightarrow L_n \uparrow \downarrow$

CASE

Fixed costs of market work t - travel time

person (A) will not work; $L_M = 0$ C - gas, ticket cost



$$l + L_H = H_0$$

(B) will work

$$l' + L_H' + L_M' = H_0 - t$$