

HUMAN

CAPITAL

# INVESTMENT IN HUMAN CAPITAL

- Assumptions:
  - investment into oneself one can increase own productivity
  - investment is also giving up of current earning

• CONTENT: simple examples

simple  
degree  
screen  
educational  
expenditure

$C_0 \dots$  current investment cost

$Y_1 \dots Y_n$  generated income

$$d_i = \frac{1}{1+r_i}$$

→ finite income stream  
→ see next page →

**CASE**

$$-C_0 + \sum_{i=1}^n d^i Y_i > 0$$

if  $r_i = r; Y_i = Y$

$$-C_0 + Y \sum d^i = -C_0 + \frac{Y}{r} (1 - d^n)$$

$$\boxed{\frac{Y}{r} (1 - d^n) > C_0} \quad \text{criterion for investment}$$

using IRR - Internal Rate of Return approach

$$\frac{Y}{r} \left( 1 - \frac{1}{(1+r)^n} \right) = C_0$$

→ find  $r^*$  and see if  $r^* > r$   
→ advantageous investment

**CASE**

$$Y_i = \bar{w} E_i \bar{H} \quad ; \quad \Delta Y = Y_1 - Y_0 = \bar{w} \bar{H} \Delta E$$

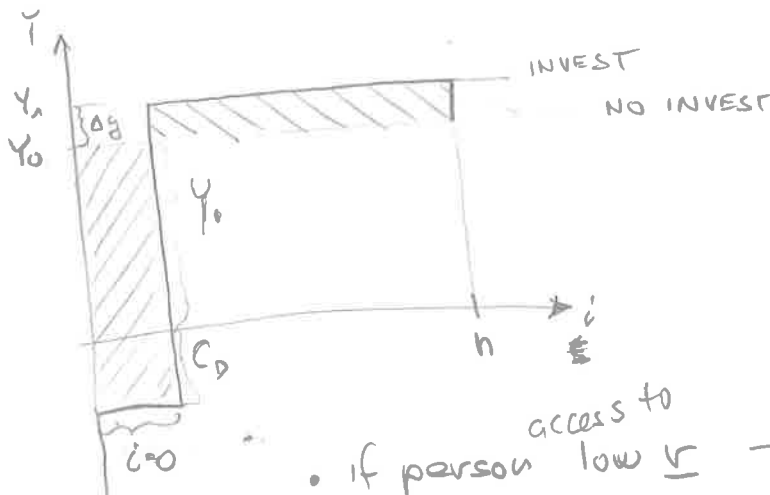
$$C_0 = C_D + Y_0$$

$H = \bar{H}$  ... hours worked

$E$  - human capital

$w = \bar{w}$  rental value of  $k = \text{wage}$

$C_0$  - cost  $\begin{cases} \text{direct} \\ \text{forgone income} \end{cases}$



$$\boxed{\frac{\Delta Y}{r} (1 - d^n) > Y_0 + C_D}$$

- if person low  $r$  →  $\frac{\Delta Y}{r} \uparrow$  → invest more
- the longer  $n$  → invest more

- invest early in career
- $C_D$  - cost of taxes

- returns to society from individual investment
- child labor

# A note on geometric series

NOTE

$$S_n = 1 + q + \dots + q^n \quad \#2$$

$$(S_{n+1} = 1 + q + \dots + q^n + q^{n+1})$$

$$qS_n = q + q^2 + \dots + q^n + q^{n+1}$$

$$= S_n - 1 + q^{n+1}$$

$$S_n = \frac{1 - q^{n+1}}{1 - q}$$

$$q = \frac{1}{1+r}$$

$$S_n = \frac{1 - \left(\frac{1}{1+r}\right)^{n+1}}{1 - \frac{1}{1+r}} = \frac{1 - \left(\frac{1}{1+r}\right)^{n+1}}{\frac{1+r-1}{1+r}} = \frac{1}{r} \left[ (1+r) - \frac{1}{(1+r)^n} \right]$$

#1

$$S_n = q + q^2 + \dots + q^n = ?$$

$$q = \frac{1}{1+r}$$

$$(S_{n+1} = \dots + q^n + q^{n+1})$$

$$qS_n = q^2 + \dots + q^n + q^{n+1}$$

$$= S_n - q + q^{n+1}$$

$$S_n = \frac{q - q^{n+1}}{1 - q} \quad \left| \quad q = \frac{1}{1+r} \right| = \frac{\frac{1}{1+r} - \left(\frac{1}{1+r}\right)^{n+1}}{\frac{r}{1+r}} = \frac{1}{r} \left[ 1 - \left(\frac{1}{1+r}\right)^n \right]$$

|||

$$\frac{1}{r} [1 - q^n]$$

Or; using #1 & #2:

$$S_n = 1 + q + \dots + q^n = \frac{1}{r} \left[ (1+r) - \frac{1}{(1+r)^n} \right] \Rightarrow$$

$$\Rightarrow S_n - 1 = \frac{1}{r} \left[ (1+r) - \frac{1}{(1+r)^n} \right] - 1 = \dots = \frac{1}{r} \left[ 1 - \left(\frac{1}{1+r}\right)^n \right]$$

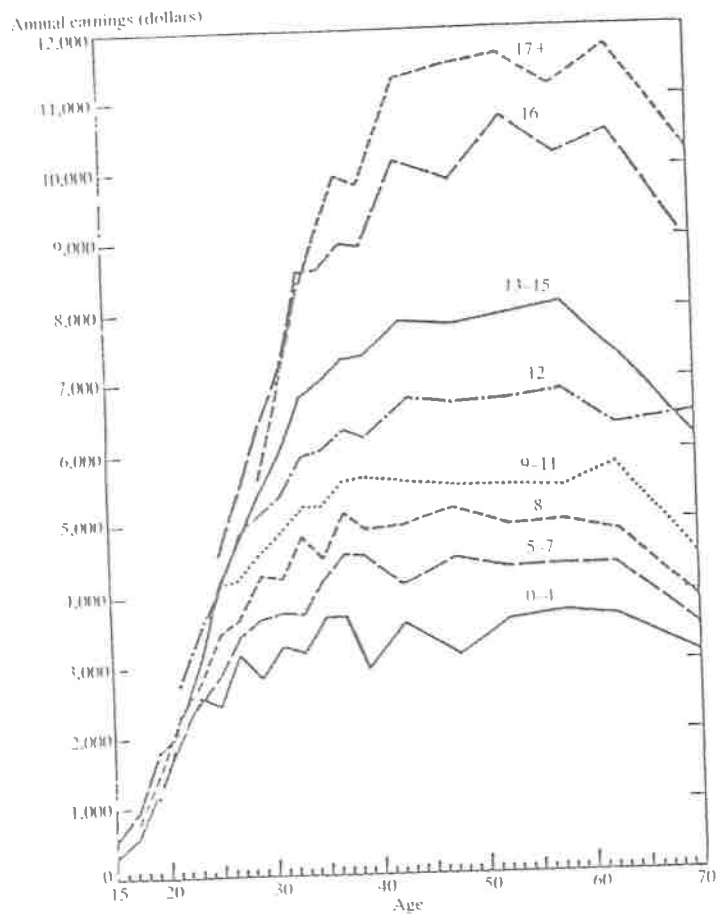


Figure 2.2 Age-earnings profiles of white non-farm men by schooling level, 1959. Source: Mincer, 1974, 66

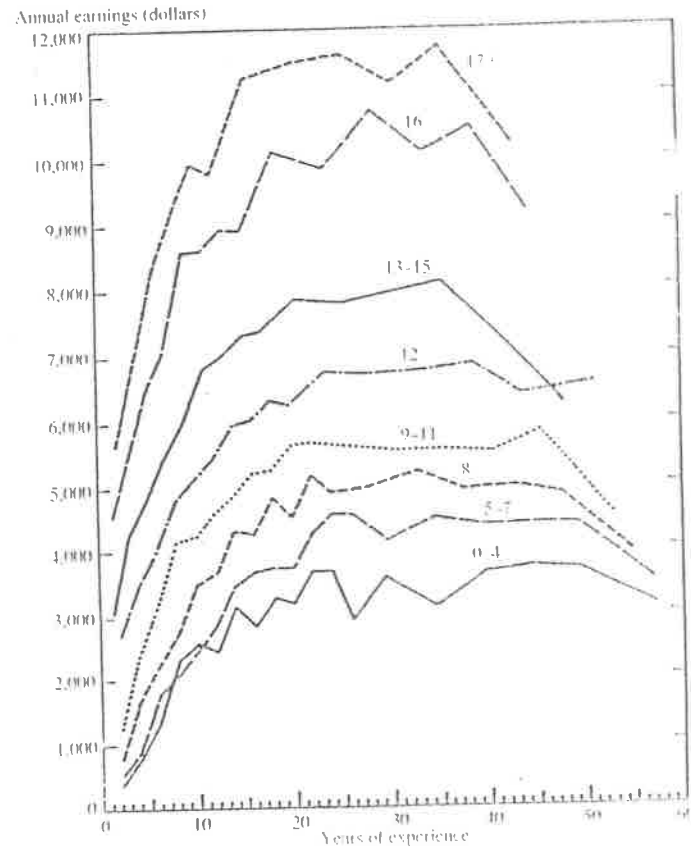


Figure 2.3 Experience-earnings profiles for white non-farm men by schooling level, 1959. Source: Mincer, 1974, 67

In figure 2.3 the two earnings patterns alluded to earlier are eminently clear: (1) earnings rise with age at a diminishing rate and (2) earnings profiles are

# Original idea of HC model - Mincer

↓  $E_t$

- At any period of life,  $t$ , decision on how to allocate a unit of time (day, year)

$0 < \phi_t < 1$ ; if  $1 - h_t \sim$  share devoted to work  $\Rightarrow Y_t = E_t (1 - h_t)$   <sup>$w=1$</sup>

$h_t$  ——— to studies:

forgone earnings (costs)

$$C_t = h_t E_t$$

increase in HC in the future

$$E_{t+1} = E_t + r C_t$$

$r > 0 \sim$  return

$$\Delta E_t = r C_t$$

$$\Delta E_t / C_t = r$$

## Questions:

- shape of life-cycle profile of  $Y_t, E_t, C_t$ ?
- decisions driving  $h_t$ ?
- shape of profile during formal schooling?
- decision driving optimal schooling?
- testable predictions?

$$E_t \equiv Y_t + C_t$$

$$E_{t+1} = E_t + r C_t$$

$$C_t = \begin{cases} E_t & \sim \text{edu} \#0 \\ c_0(1 - \frac{t}{T}) & \sim \text{version} \#1 \\ b_0(1 - \frac{t}{T}) E_t & \sim \text{version} \#2 \end{cases}$$

$$\frac{dE_t}{dt} = r C_t \rightarrow dE_t = r C_t dt$$

$$\#0 \quad dE_t = r E_t dt$$

$$\frac{dE_t}{E_t} = r dt$$

$$\int \frac{dE_t}{E_t} \equiv \ln E_t = r \cdot S + E_0$$

$$\#2 \quad dE_t = r b_0(1 - \frac{t}{T}) E_t$$

$$\frac{dE_t}{E_t} = r b_0(1 - \frac{t}{T})$$

$$\int \frac{dE_t}{E_t} \equiv \ln E_t = r b_0 \underline{\underline{EXP}} - r b_0 \frac{t}{2T} \underline{\underline{EXP^2}} + E_0$$

$$Y_t = E_t - C_t = E_t [1 - b_0(1 - \frac{t}{T})]$$

$$\ln Y_t \approx \ln E_t - b_0(1 - \frac{EXP}{T})$$

$$\ln Y_t = \text{const}_1 + \beta \cdot S + \delta_1 \text{EXP} + \delta_2 \text{EXP}^2$$

Sample of Mincer regression coefficients

	Coefficient on EXP	100*Coefficient on EXP2	Years of maximum returns from experience	Average years of schooling 1995	Coefficient on EDU	Period
Argentina	0.052	-0.07	37.1	0	0.11	1989
Austria	0.039	-0.067	29.1	11.9	0.04	1987
Bolivia	0.046	-0.06	38.3	0	0.07	1989
Brazil	0.073	-0.1	36.5	5.3	0.15	1989
Britain	0.091	-0.15	30.3	12.1	0.10	1972
Canada	0.025	-0.046	27.2	13.2	0.04	1981
Chile	0.048	-0.05	48.0	0	0.12	1989
China	0.019	0	n.a.	0	0.05	1985
Colombia	0.059	-0.06	49.2	0	0.15	1989
Czech R.	0.021	-0.04	26.3	12.5	0.03	Men, 1989
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Czech R.	0.028	-0.059	23.7	0	0.04	1988
Czech R.	0.032	-0.063	25.4	0	0.09	1996
Denmark	0.033	-0.057	28.9	12.4	0.05	1990
Ecuador	0.054	-0.08	33.8	0	0.10	1987
Greece	0.039	-0.088	22.2	10.9	0.03	1985
Guatemala	0.044	-0.06	36.7	0	0.14	1989
Hungary	0.034	-0.059	28.8	11.3	0.04	1987
India	0.041	-0.05	41.0	0	0.06	1981
Indonesia	0.094	-0.1	47.0	0	0.17	1981
Ireland	0.061	-0.1	30.5	10.8	0.08	1987
Israel	0.029	-0.046	31.5	0	0.06	1979
Italy	0.01	-0.027	18.5	10	0.03	1987
Kenya	0.044	-0.2	11.0	0	0.09	1986
South Korea	0.082	-0.14	29.3	0	0.11	1986
Malaysia	0.013	-0.004	162.5	0	0.09	1979
Mexico	0.084	-0.1	42.0	0	0.14	1984
Netherlands	0.035	-0.049	35.7	12.7	0.07	1983
Pakistan	0.106	-0.06	88.3	0	0.10	1979
Poland	0.021	-0.036	29.2	11.1	0.02	1986
Portugal	0.025	-0.04	31.3	10	0.09	1985
Singapore	0.062	-0.1	31.0	0	0.11	1974
Spain	0.049	-0.06	40.8	11.2	0.13	1990
Sweden	0.049	0	n.a.	12.1	0.03	1981
Switzerland	0.056	-0.069	40.6	12.6	0.07	1987
Thailand	0.071	-0.088	40.3	0	0.09	1971
USA	0.032	-0.048	33.3	13.5	0.09	1989
West Germany	0.045	-0.077	29.2	13.4	0.08	1988
AVERAGE	0.049	-0.069	42.9	11.6	0.09	-