

• INTRODUCING HOUSEHOL ECONOMY

Bodelv: "Not necessary change in preferences but a in the opportunity cost of time"

MODEL

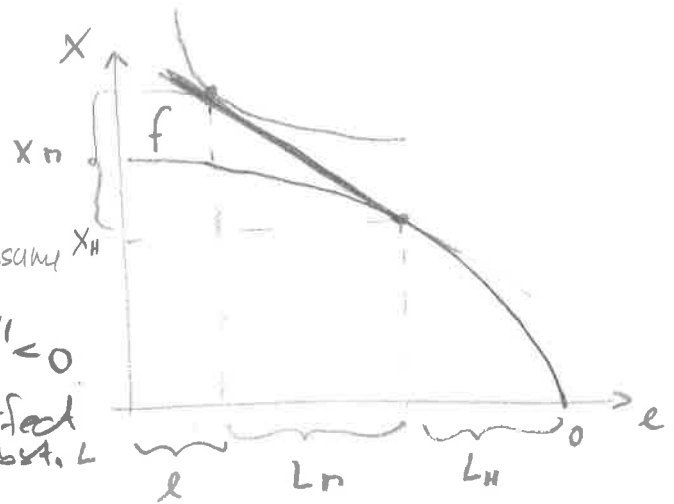
$$u = u(x, l)$$

$$x = x_H + x_n + x_o, p = 1$$

$$T = l + L_H + L_n \quad \rightarrow \frac{\partial f}{\partial x_n} = 0 \text{ assume } x_H$$

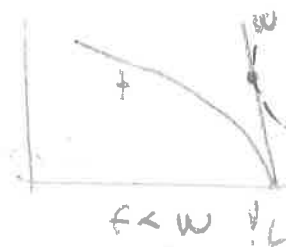
$$x_H = f(L_H) \quad ; \quad f' > 0, f'' < 0$$

$$x_H = \dots + wL_n \quad ; \quad x_H \& x_n \text{ perfect subst. } L$$

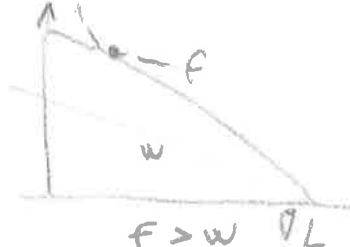


What affects participation - on the L_n?

$$f' \stackrel{?}{\gtrless} w$$



f < w ! L
①



f > w ! L
②



f = w
③

FONC in CASE ③

$$\frac{\partial u / \partial l}{\partial u / \partial x} = w = \frac{\partial f}{\partial L_n} = \frac{\partial u / \partial L_n}{\partial u / \partial x} = \frac{\partial u / \partial L_n}{\partial u / \partial x}$$

~~READING~~

$$\mathcal{L}(x, l, \mu, \lambda) = u(x, l) + \lambda [x_o + wL_n + f(L_H) - x] + \mu [T - l - L_n - L_H]$$

$$\left. \begin{aligned} u_x - \lambda &= 0 \\ u_l - \mu &= 0 \end{aligned} \right\} \frac{u_l}{u_x} = \frac{\mu}{\lambda} = f' = w$$

$$\left. \begin{aligned} \lambda w - \mu &= 0 \\ \lambda f' - \mu &= 0 \end{aligned} \right\} \frac{w}{f'} = 1 \rightarrow w = f'$$

$$f' = \frac{\mu}{\lambda}$$

-w > w

You have 1 unit of time Δt to be used in three ways: l, l_H, l_M

leisure: $\Delta t \rightarrow \Delta l \rightarrow \Delta U^l = \frac{\partial U}{\partial l} \Delta t$ (i)

X home: $\Delta t \rightarrow \Delta l_H \rightarrow \Delta U^H = \frac{\partial U}{\partial X} \frac{\partial X}{\partial l_H} \Delta t$
 $= \frac{\partial U}{\partial X} f' \Delta t$ (ii)

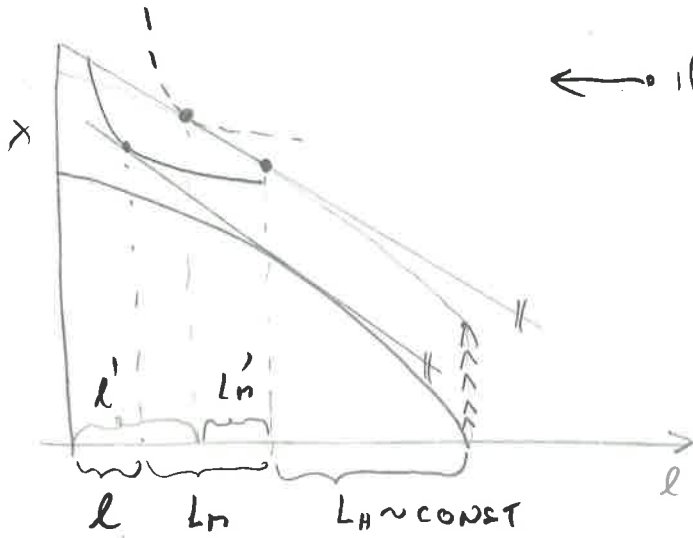
X work: $\Delta t \rightarrow \Delta l_M \rightarrow \Delta U^M = \frac{\partial U}{\partial X} w \frac{\Delta t}{p}$ (iii)

(i) & (ii): $\frac{\partial U}{\partial l} = f'$

(i) & (iii): $\frac{\partial U}{\partial l} = \text{MRS}_{l, X} = w$

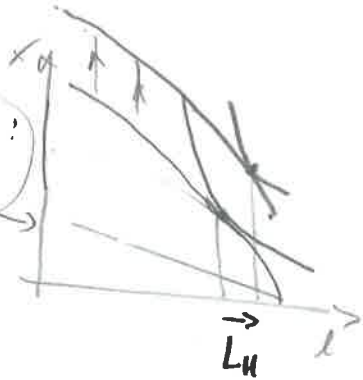
(ii) & (iii): $f' = w / p$

CASE Increase in non-labor income X_0

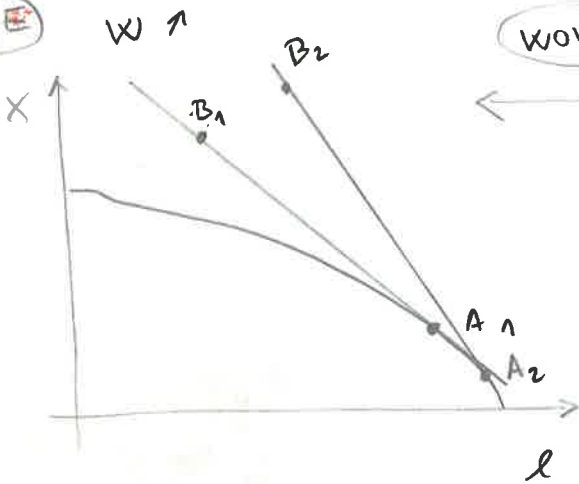


← if NORMAL GOOD, L_H will stay const.
 $\uparrow l'$
 $\downarrow L_n$

if not on the LM:
 $L_H \downarrow, l \uparrow$



CASE



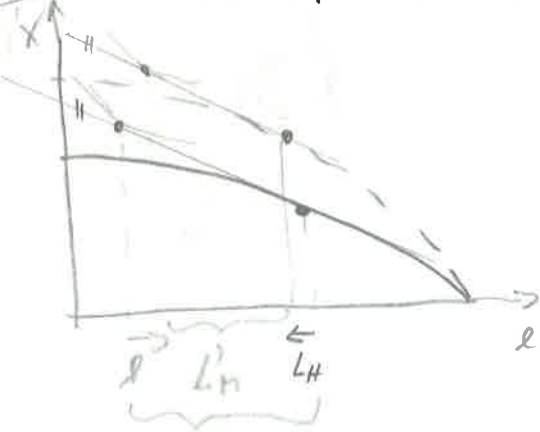
working person

• $L_H \downarrow, L_n ? , l ?$

if not on the LM

• $\uparrow W \Rightarrow$ no effect or participation
 $L_H \downarrow, l ?, L_n ?$

CASE Growth of home productivity (weed medicine, vacuum cleaner)



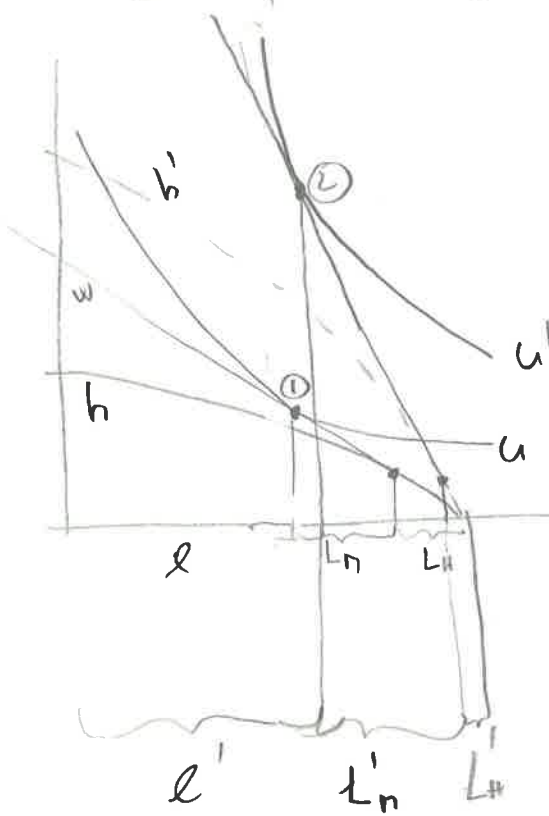
$L_H \uparrow, L_n \downarrow, l \uparrow$

but empirically, we observe $L_H \downarrow$
 why?

CASE SCHOOLING - increases not only w but also shift $f(L_H) \uparrow$

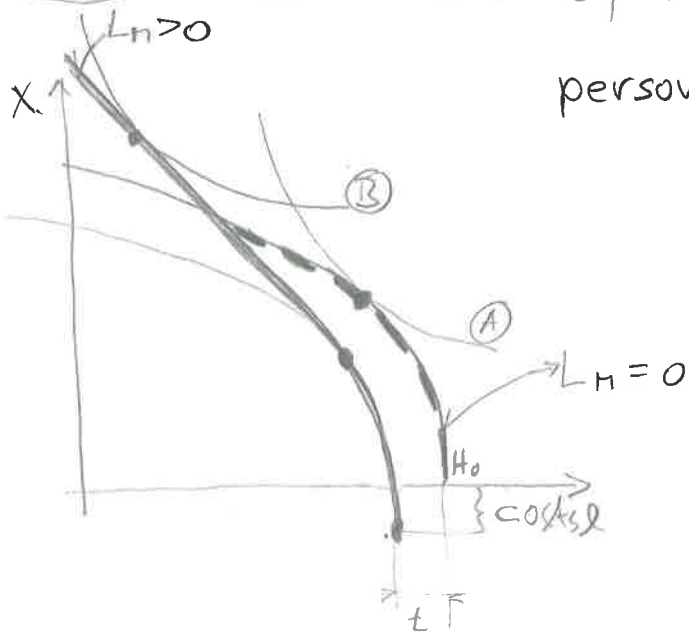
CASE Change in home and market productivity during decades $\Delta x / \Delta L_M, \Delta x / L_H \nearrow$

① Change in $\Delta x / \Delta L_H$



- $\Delta L_H \nearrow$ if $\Delta w \nearrow \Rightarrow \Delta T \nearrow \Delta L_H$
- ΔL_n & Δl depend on income & subst. eff.
- $l \nearrow$ if subst $>$ income eff.
 $\hookrightarrow L_n \nearrow$
- $l \nearrow$ if subst $<$ income eff.
 $\hookrightarrow L_n \downarrow$

CASE Fixed costs of market work t - travel time
 person A will not work; $L_M = 0$ C - gas, ticket cost



$$l + L_H = H_0$$

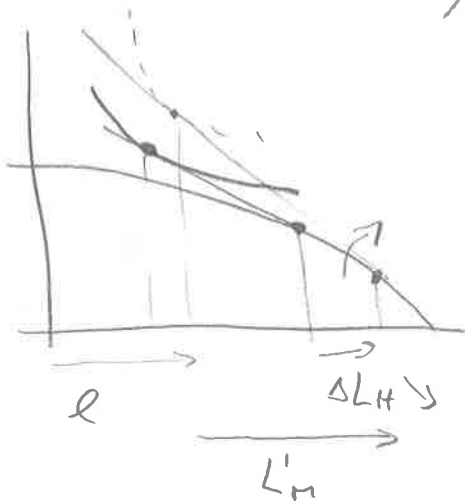
③ will work

$$l' + L_H' + L_M' = H_0 - t$$

• CHILD-CARE PROGRAMS: enhance L_H & L_M part of women

↳ impact on $MRS_{x vs. e}$
 F, F'

CASE Subsidy for every hour worked ~ opposite of taxation
 $\Rightarrow \uparrow W: L_H \downarrow; \Delta L_M \text{ \& \; } \Delta e ?$



• original policy purpose is not certain in case of working women

• is certain in case of not-working women if subsidy high.

CASE Lump-sum subsidy

\equiv free child-care

C ~ cost of child-care

Women (A, B, C)

(A) $L_H = \text{const}, L_M \downarrow, e \uparrow$ (-)

(B) $L_H \downarrow, L_M \uparrow, e \downarrow$ (+)

(C) $L_H = \text{const}, L_M = 0, e = \text{const}$

