Problem 1: A Firm has the following production function: $Q=\sqrt{K L}$. Further we know that $w=36$ and $r=9$.
(a) Derive short run cost function when the amount of capital is fixed: $\bar{K}=9$
(b) Derive long run cost function

Problem 2: Total cost function of an individual firm facing perfect competition is given by relation:

$$
T C(Q)=Q^{3}-20 Q^{2}+150 Q
$$

Find the optimal level of production (supply function) of this firm. For what prices would the firm earn a positive profit? Negative profit? Zero profit?

Problem 3: The demand for oranges is $q=120-4 p$ and the supply is $q=2 p-30$, where $p$ is the price measured in dollars per hundred pounds and $q$ is the quantity measured in hundred pound units.
(a) On one graph, draw the demand curve and the supply curve for oranges.
(b) Write down the equation that you would solve to find the equilibrium price.
(c) What is the equilibrium price of oranges? What is the equilibrium quantity? Show the equilibrium price and quantity on the graph and label them $p_{1}$ and $q_{1}$.
(d) A terrible drought strikes California, traditional homeland of oranges. The supply schedule shifts to $2 p-60$. The demand schedule remains as before. Draw the new supply schedule. Write down the equation that you would solve to find the new equilibrium price of oranges.
(e) What is the new equilibrium price of oranges? What is the new equilibrium quantity? Show the equilibrium price and quantity on the graph and label them $p_{2}$ and $q_{2}$.

