# Intermediate Microeconomics <br> Uncertainty and Information 

Agribusiness Teaching Center
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## Tacit Collusion

## Cartels

## Fact

In order to make extra-normal (half monopoly level) profit, the producers may collude on price.

## Example

|  | Honour Agreement |  | Cheat |  |
| :---: | :---: | :---: | :---: | :---: |
| Honour Agreement | $£ 1000$ | $£ 1000$ | $£ 200$ | $£ 1200$ |
| Cheat | $£ 1200$ | $£ 200$ | £ 500 | $£ 500$ |

- Simultaneous game
- Sequential game


## Mixed strategy

Matching pennies

## Player 2

|  |  | Heads |  |
| :---: | :--- | :---: | :---: |
| Tails |  |  |  |
| Player 1 | Heads | $1,-1$ | $-1,1$ |
|  | Tails | $-1,1$ | $1,-1$ |
|  |  |  |  |

There is no (pure strategy) Nash equilibrium in this game. If we play this game, we should be "unpredictable." That is, we should randomise (or mix) between strategies so that we do not get exploited.

## Mixed Equilibrium and Dominated Strategies



## Expected Utility

| Outcome | Prob | Utiliy |
| :--- | :--- | :--- |
| $X$ | $p$ | $U(X)$ |
| $Y$ | $1-p$ | $U(Y)$ |

## Expected Utility

$$
\mathrm{E} U=p \cdot U(X)+(1-p) \cdot U(Y)
$$

## Lotteries

- Suppose you had to choose between two lotteries:
$-L_{1}$ :
* win $\$ 1$ million for sure
$-L_{2}$ :
* win $\$ 5$ million w.p. 0.1
* win $\$ 1$ million w.p. 0.89
* win $\$ 0$ w.p. 0.01
- Which one would you choose?
- Which one should you choose?


## Lotteries

- Suppose you had to choose between two lotteries:
- $L_{1}$ :
* win $\$ 1$ million for sure
- $L_{2}$ :
* win $\$ 5$ million w.p. 0.1
* win $\$ 1$ million w.p. 0.89
* lose $\$ 1$ million w.p. 0.01
- Which one would you choose?
- Which one should you choose?


## Lotteries

- Suppose you had to choose between two lotteries:
- $L_{1}$ :
* \$5 million w.p. 0.1
* \$0 w.p. 0.9
- $L_{2}$ :
* $\$ 1$ million w.p. 0.3
* \$0 w.p. 0.7
- Which one would you choose?
- Which one should you choose?


## Risk and Preferences

- Capture preferences towards rewards and resource consumption
- Capture risk attitudes
E.g. if one is risk-neutral, getting $\$ 5$ million has exactly half the utility of getting \$ 10 million
- People are generally risk-averse when it comes to money


Risk Neutral
(= Expected reward)


Risk Averse


Risk Seeking

## Expected Utility and Risk

- Either 35 or 20 income

- Equal probabilities
- Expected utility
- Risk neutral, averse, or loving
- Fair gamble
- Actuarially fair insurance


## Risk and Insurance



- Actuarially fair insurance
- Willingness to pay
- Adverse selection
- Moral Hazard


## Value of Information

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- Whene theystaldinary


## Value of information

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- Two blocks A and B, exactly one has oil, worth $k$
- Prior probabilities 0.5 each, mutually exclusive
- Current price of each block is $\mathrm{k} / 2$
- Consultant offers accurate survey of $A$
- What is a fair price for the survey?

Survey may say "oil in A" or "no oil in A", with probability 0.5 each, so the value of the information is: [ $0.5 \times$ value of "buy $A$ " given "oil in A" $+0.5 \times$ value of "buy B" given "no oil in A"] - $0=(0.5 \times k / 2)+$ $(0.5 \times \mathrm{k} / 2)-0=\mathrm{k} / 2$

## Internal Organisation <br> Contract Theory

## Fact (Moral Hazard)

Unmonitored workers of a firm tend to shirk their duties.

## Definition

Moral Hazard is opportunism characterised by an informed person's taking advantage of a less-informed person through an unobserved action.

## Fact

An architect working for 'percentage' of the deal will overdecorate.

## Fact

A lawer working for 'percentage' will do his best to assure the best deal for the contractor.

## Internal Organisation

## Problem

Worker's utility:

$$
u(w, e)=w-\delta(e)
$$

where $w$ is the wage and $\delta(e)$ is the disutility of working with an effort level e.
The probability of being caught while shirking: $p$.
Shirks if

$$
E \mathbb{U}\left(e=e_{\text {shirk }}\right)>E \mathbb{U}\left(e=e^{*}\right)
$$

Wage while caught shirking is $w_{-}$and otherwise is $w^{*}$

## Internal Organisation

## Problem

Worker's utility: $u(w, e)=w-\delta(e)$

- Expected utility while not shirking:

$$
E \mathbb{U}\left(e=e^{*}\right)=w^{*}-\delta\left(e^{*}\right)
$$

- Expected utility while shirking:

$$
E \mathbb{U}\left(e=e_{\text {shirk }}\right)=p \cdot w^{-}+(1-p) \cdot w^{*}-\delta\left(e_{\text {shirk }}\right)
$$

Assume $\delta\left(e_{\text {shirk }}\right)=0$

## Internal Organisation

## Problem

Shirks if

$$
\begin{aligned}
E \mathbb{U}\left(e_{\text {shirk }}\right) & >E \mathbb{U}\left(e=e^{*}\right) \\
p \cdot w^{-}+(1-p) \cdot w^{*} & >w^{*}-\delta\left(e^{*}\right)
\end{aligned}
$$

Non-shirking condition is

$$
w^{-}-w^{*}>\frac{\delta\left(e^{*}\right)}{p}
$$

## Efficient Risk-sharing Principal - Agent Problem

## Definition

Efficient contract is an agreement with provision that ensure that no party can be made better off without harming the other party.

## Fact

Any contract should:

- be Incentive Compatible (so that the agent wants to perform the assigned task rather than engage in opportunistic bahaviour,
- satisfy Participation Constraint (so that the agent would want to sign the contract).


## Principal - Agent Problem

Perfectly observable Action

## Problem (of the Agent)

Utility:

$$
u(e, w)=w(e)-\delta(e)
$$

Levels of effort:

$$
e=\left\{e_{H}, e_{L}\right\}
$$

## Principal - Agent Problem Perfectly observable Action

## Problem (of the Principal)

Profit: $\pi(e)=R(e)-w(e)$
Revenue probability matrix (conditional on effort level):


Expected Revenue:

$$
\begin{aligned}
& E R\left(e_{H}\right)=p^{h} \cdot R^{+}+\left(1-p^{h}\right) \cdot R^{-} \\
& E R\left(e_{L}\right)=p^{\prime} \cdot R^{+}+\left(1-p^{\prime}\right) \cdot R^{-}
\end{aligned}
$$

## Principal - Agent Problem

## Perfectly observable Action

## Problem (Stage 1)

$$
\min w\left(e_{H}\right)
$$

subject to

$$
\begin{array}{ll}
w\left(e_{H}\right)-\delta\left(e_{H}\right) \geqslant \bar{w} & \text { Participation Constraint } \\
w\left(e_{H}\right)-\delta\left(e_{H}\right) \geqslant w\left(e_{L}\right)-\delta\left(e_{L}\right) & \text { Incentive Compatibility }
\end{array}
$$

## Problem (Stage 2)

Compare expected profits:

$$
E \pi\left(e_{H}\right) \text { and } E \pi\left(e_{L}\right)
$$

## Principal - Agent Problem <br> Unobservable Action

## W hat if the actions are not observable?

## Principal - Agent Problem <br> Unobservable Action

- Wages are conditional on the outcome:

$$
w=\begin{array}{ll}
w^{G} & \text { if revenue is } R^{+} \\
w^{B} & \text { if revenue is } R^{-}
\end{array}
$$

## Fact

In case the actions of Agent are observable, all of the risk is taken by the Principal.
In case of unobservable actions, the risk is shared between the Principal and the Agent.

## Principal - Agent Problem <br> Unobservable Action

## Problem (Stage 1: Motivating for high effort)

$$
\min p^{h} w^{G}+\left(1-p^{h}\right) w^{B}
$$

subject to

$$
\begin{array}{ll}
p^{h} w^{G}+\left(1-p^{h}\right) w^{B}-\delta\left(e_{H}\right) \geqslant \bar{w} & P C \\
p^{h} w^{G}+\left(1-p^{h}\right) w^{B}-\delta\left(e_{H}\right) \geqslant p^{\prime} w^{G}+\left(1-p^{\prime}\right) w^{B}-\delta\left(e_{L}\right) & I C
\end{array}
$$

## Problem (Stage 2)

Compare expected profits:

$$
E \pi\left(e_{H}\right) \text { and } E \pi\left(e_{L}\right)
$$

