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# Economic Development

Population

November 2010

## Definition (**Fertility**)

The quality of being able to produce young

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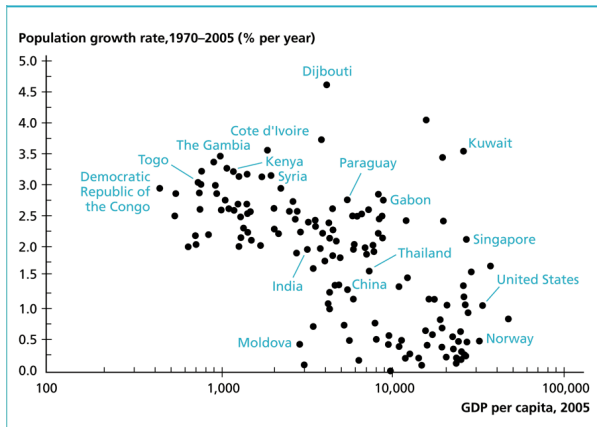
## Fact

*'With every mouth God sends a pair of hands.'*

*An old saying*

# Growth and Fertility Development

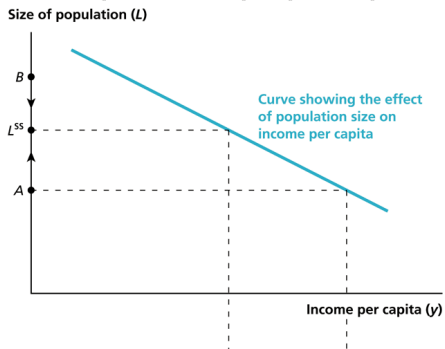
## Facts



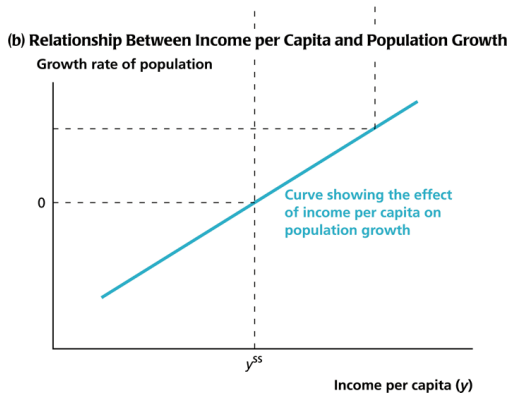
Source: Heston et.al. (2006), World Bank (2007a).

# Malthus Theory

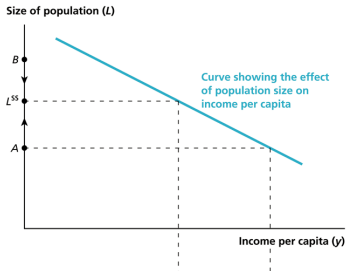
(a) Relationship Between Income per Capita and Population Size



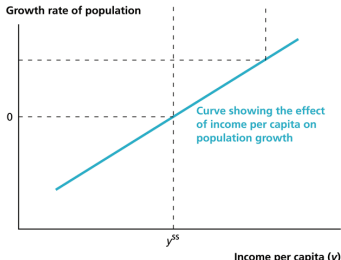
# Malthus Theory



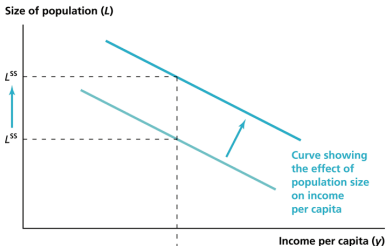
(a) Relationship Between Income per Capita and Population Size



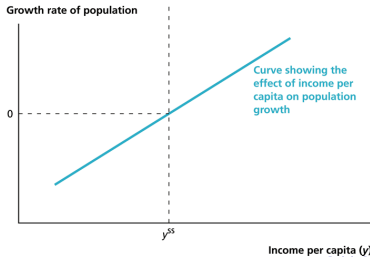
(b) Relationship Between Income per Capita and Population Growth



**(a) Relationship Between Income per Capita and Population Size**



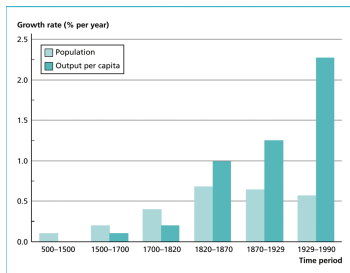
**(b) Relationship Between Income per Capita and Population Growth**



## Corollary

*Unless 'passion between sexes' is suppressed, the human race is doomed to breed itself into poverty.*

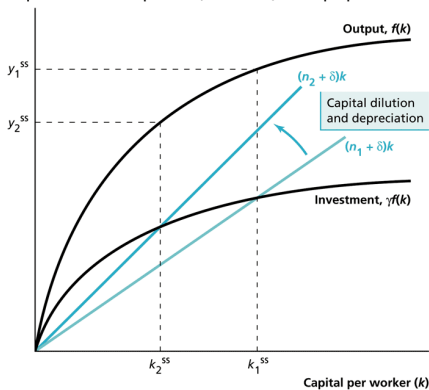
## Fact



Source: Galor and Weil (2000).



Capital dilution and depreciation, investment, and output per worker



### Capital Dilution

$$\Delta K = s \cdot F(K, L) - \delta K$$

Per capita

$$\Delta k = s \cdot f(k) - (\delta + n) k$$

steady state  $\Delta k = 0$

$$s \cdot f(k_{ss}) = (\delta + n) k_{ss}$$

## Quantitative Analysis

$$f(k) = Ak^\alpha$$

$$k_{ss} = \left(\frac{sA}{n+\delta}\right)^{\frac{1}{1-\alpha}}$$

$$\frac{y_{ss}^A}{y_{ss}^B} = \left(\frac{n_B + \delta}{n_A + \delta}\right)^{\frac{\alpha}{1-\alpha}}$$

$$sAk^\alpha = (\delta + n)k$$

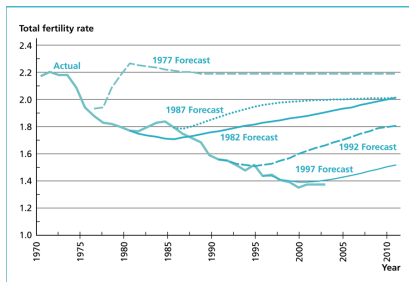
$$y_{ss} = A^{\frac{1}{1-\alpha}} \left(\frac{sA}{n+\delta}\right)^{\frac{1}{1-\alpha}}$$

$$\frac{y_{ss}^A}{y_{ss}^B} \stackrel{\alpha=\frac{1}{3}}{=} \left(\frac{0,04 + 0,05}{0,00 + 0,05}\right)^{1/2} = 1,34$$

## Corollary

*Higher population growth dilutes the per-worker capital stock more quickly and so lowers the steady-state level of output per worker.*

## Fact

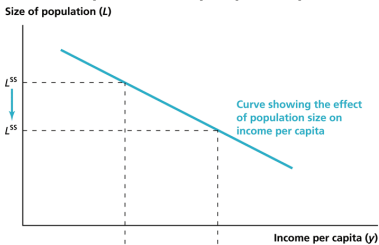


Source: Yashiro (1998).

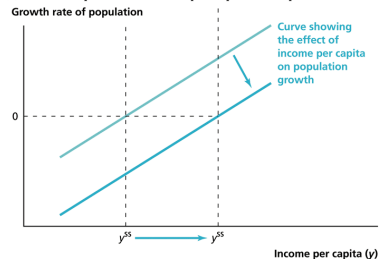
- ▶ Child Labour
- ▶ Old-age Insurance
- ▶ Tandem Effect
- ▶ Family Planning (Malthus)
- ▶ Income and Substitution Effects for Female labor
- ▶ Quality-quantity Tradeoff

- └ Growth Correlates: Fertility
- └ Explaining reduced fertility (Malthus)

(a) Relationship Between Income per Capita and Population Size



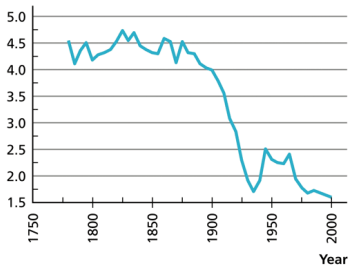
(b) Relationship Between Income per Capita and Population Growth



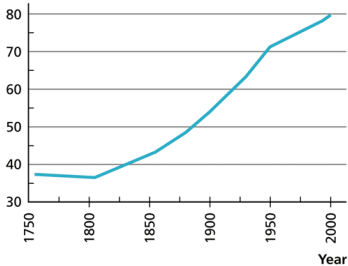


- └ Growth Correlates: Fertility
- └ Explaining reduced fertility (Tandem)

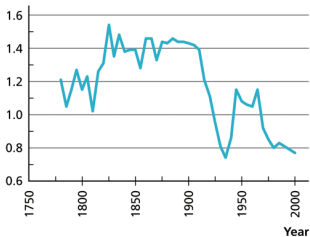
(a) Total Fertility Rate



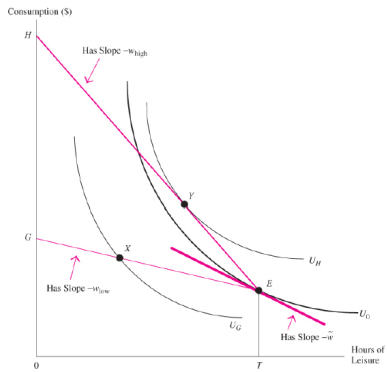
(b) Life Expectancy at Birth



(c) Net Rate of Reproduction



└ Growth Correlates: Fertility  
└ Female Labour Participation





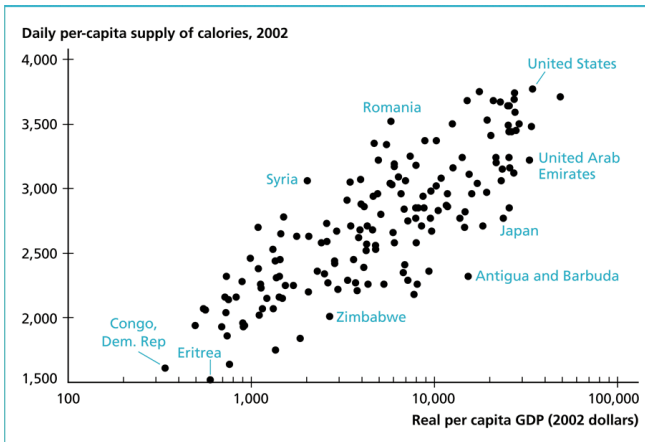
# Human Capital

## Definition

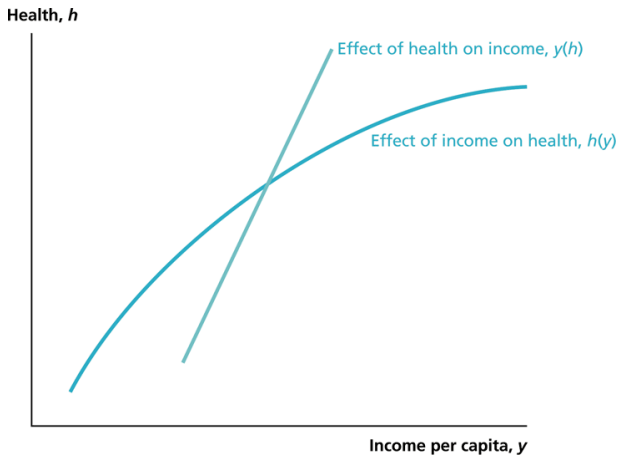
Human capital refers to the stock of competences, knowledge and personality attributes embodied in the ability to perform labor so as to produce economic value.

© Wikipedia

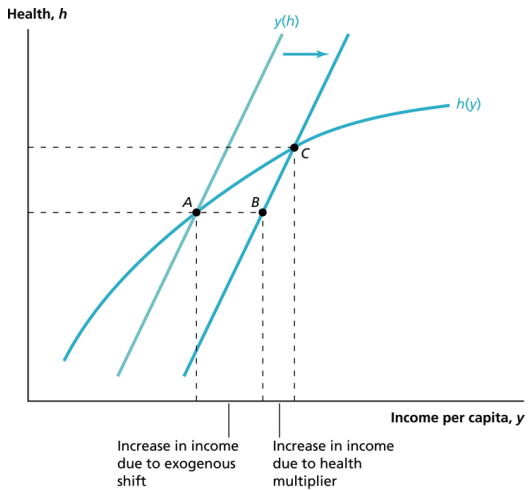
- ▶ Health
- ▶ Education



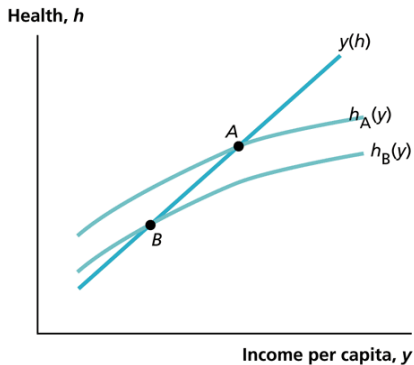
Sources: FAOSTAT database, Heston, Summers, and Aten (2006).



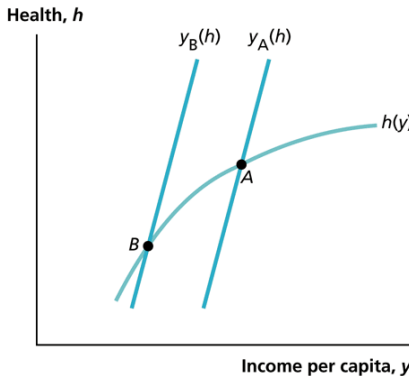
└ Growth Correlates: Human Capital  
└ Health and Income



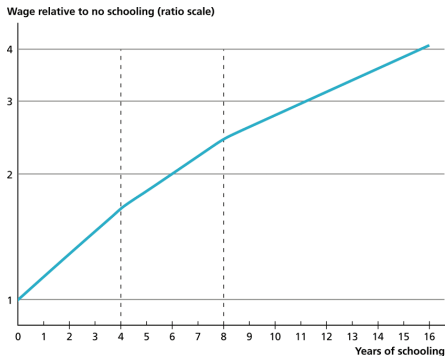
(a) The Health View



(b) The Income View

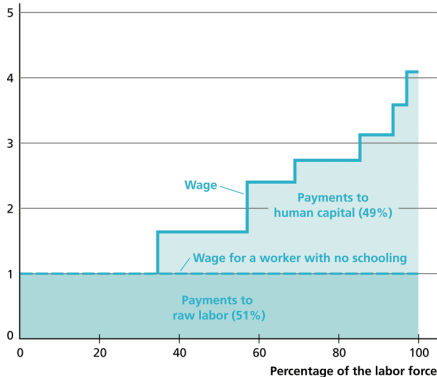


## Returns to Education

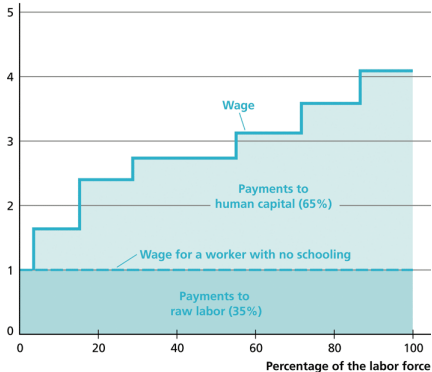


# Human Capital's Share of Wages

Wage relative to no schooling



Wage relative to no schooling



## Quantitative Analysis

$$Y = AK^\alpha (hL)^{1-\alpha}$$

$$Y = (h^{1-\alpha}A) K^\alpha L^{1-\alpha}$$

From before:

$$y_{ss}^{OLD} = A^{\frac{1}{1-\alpha}} \left( \frac{s}{n+\delta} \right)^{\frac{\alpha}{1-\alpha}}$$

Now:

$$\begin{aligned} y_{ss} &= (h^{1-\alpha}A)^{\frac{1}{1-\alpha}} \left( \frac{s}{n+\delta} \right)^{\frac{\alpha}{1-\alpha}} \\ &= h \times \left[ A^{\frac{1}{1-\alpha}} \left( \frac{s}{n+\delta} \right)^{\frac{\alpha}{1-\alpha}} \right] \end{aligned}$$



## Quantitative Analysis

$$\frac{y_{ss}^A}{y_{ss}^B} = \frac{h_A \times \left[ A^{\frac{1}{1-\alpha}} \left( \frac{s}{n+\delta} \right)^{\frac{\alpha}{1-\alpha}} \right]}{h_B \times \left[ A^{\frac{1}{1-\alpha}} \left( \frac{s}{n+\delta} \right)^{\frac{\alpha}{1-\alpha}} \right]} = \frac{h_A}{h_B}$$

## Corollary

*The difference in incomes is fully explained by the difference in the human capital.*

## Fact

