The Quarterly Projection Model

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Outline

1. Trend and cycles
2. Structure of the Quarterly Projection Model
3. Parameters setup
4. Properties of the Model
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1. Trend and cycles
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Trend and cycles

Time series analysis

- Analysis of time series data is based on smoothing past data in order to separate the underlying pattern in the data series from randomness.
- The underlying pattern then can be projected into the future and used as the forecast.
- The underlying pattern can also be broken down into sub patterns to identify the component factors that influence each of the values in a series: decomposition.
- Decomposition methods: identify separate components of the basic underlying pattern that tend to characterize economics and business series.
In search for trends

Dogbert Consults:

You need to do data mining to uncover hidden sales trends.

If you mine the data hard enough, you can also find messages from God.

...sales to left-handed squirrels are up...and God says your tie doesn't go with that shirt.
Decomposition Techniques

- Goal: separation of data into several unobservable components, generally in an additive or multiplicative form.
- Components: trend, seasonal pattern, cycle, and residual or irregular pattern
- Seasonal component: the periodic fluctuations of constant length
- Trend-cycle component: long term changes in the level of series
Detrending

- Trend Component: The tendency of a variable to grow over time, either positively or negatively.
- Basic forces in trend: population change, price change, technological change, productivity change, product life cycles
- The long-term movements or trend in a series can be described by a straight line or a smooth curve.
- The long-term trend is estimated from the seasonally adjusted data for the variable of interest
- Interpretation:
  - Trends: long run equilibrium
  - Gaps: cyclical fluctuations
Trend analysis

- Assume seasonally adjusted data
- Trend-Cycle decomposition: Series = Trend + Cycle + Noise
- No general-automatic techniques for detrending
- Simple techniques: Smoothing
  - Moving average: The average eliminate some higher frequency noise in the data, and leaves a smooth trend-cycle component. What order to use?
  - Simple centered moving average: can be defined for any odd order. A moving average of order k, is defined as the average consisting of an observation and the $m = (k-1)/2$ points on either side.
  - Centered moving average: take the simple centered moving average, assign weights and create weighted average
- Advanced techniques of detrending:
  - Fitting a polynomial
  - Using a structural model
Detrending techniques overview I

- Watson detrending: greater business cycle persistence; trend component follows a random walk with drift and cyclical component is a stationary finite order AR process.
- Harvey-Clark detrending: local linear trend model
- Hodrick-Prescott filter: univariate method
- Kalman filter: multivariate method, structural method
- Bandpass filter: not widely used, frequency domain analysis
Detrending techniques overview II

- Detrending comparison: US GDP gap
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Motivation for QPM

- Separate econometric methods: Inconsistencies
- Short experience with FPAS: Forecasting and Policy Analysis System
- State:
  - Insufficient data and experience to support advanced model
  - Need to increase participation of other departments and bank board
  - Communication of results: support for decision
  - Need for research tool
- The further step on the way to complex structural models: DSGE
Features of QPM

- Reflects inflation targeting regime:
  - In December 1997: after an exchange rate crisis
  - CNB adopted a series of end-year inflation targets
  - Regime proved very effective in combating inflation and anchoring
  - Evolution toward a more transparent inflation targeting regime where monetary policy is anchored by a medium-term perspective
  - Change to point inflation target: Inflation target band
  - The character of the regime was further enhanced by publication of unconditional forecasts

- Linked to quarterly data

- Small open-economy gap model
Model of trends and cycle

- Two separate blocks:
  - Long run equilibrium trends
  - Cyclical fluctuations - gaps
  - These blocks are separable
  - Super-neutrality: no long-run trade-off between output and inflation

- 85 equations at start

- Further extensions
Long Run Trends

• First step: filter trend series
  ▶ History - estimated by a simple statistical model (Kalman filter) and expert judgement
  ▶ Forecast - exogenous (expert judgement), respecting steady state properties of QPM

• Important equilibrium values:
  ▶ Real output growth
  ▶ Real wage growth
  ▶ Real exchange rate appreciation
  ▶ Real interest rate
  ▶ Stationarity is required: growth rates in focus

• Monetary decisions have small impact on long term real trends
Cyclical Part of QPM

- Description of the position of the Czech economy
- Monetary policy characteristics:
  - Inflation targeting regime
  - Forward looking policy
  - Focus on deviations from the target → reaction to expected inflation a year ahead
  - Floating exchange rate - endogenous
- Description of behavior economic agents includes forward looking components
- Price frictions:
  - Wage stickiness
  - Final price stickiness
  - Expectation stickiness
Scheme of model

Exchange rate

Monetary policy interest rate

Real monetary conditions

Long-term interest rates

Output

Real marginal cost

Real wage

Inflation

Inflation expectations

Nominal wage growth
Real Economy I

IS curve (Aggregate demand):

- Output: function of lagged output, the real interest rate, the real exchange rate and foreign demand and interest rate
- Includes impact of a change in interest rates with longer maturity on aggregate demand and take into account expectations about yield-curve on the dynamic properties of the model
- Real impact of monetary policy in a sticky-price model of a small open economy
- Marginal costs: cost of producing additional unit of a good
Real Economy II

Real Marginal Costs Gap:

- Approximation of inflationary pressures from the real economy.
- Marginal costs consist of the costs arising from the increasing volume of production (the "output gap") and wage costs (the "real wage gap").
- A positive real marginal cost gap implies an inflationary effect of the real economy

\[ \hat{mc}_t = \lambda \hat{y}_t + \hat{wr}_t \]
Real Economy III

Output Gap:

- Standard economic theory: higher real interest rate reduce aggregate demand by increasing the reward to saving
- Output gap: responds negatively to the difference between the real interest rate and its equilibrium value
- Open economy: the exchange rate matters
- Currency appreciation will, all else equal, make domestic goods more expensive in foreign markets and reduce demand for domestic goods abroad; cheaper imports may displace domestic goods

\[
\begin{align*}
\hat{y}_t &= \alpha_1 \hat{y}_{t-1} - \text{rmci}_{t-1} + \alpha_2 \hat{y}_f + \varepsilon_t \\
\text{rmci}_t &= \beta_1 \left( \beta_3 \hat{r}_c_t + \beta_4 \hat{r}_4 + (1 - \beta_3 - \beta_4) \hat{r}_4^f \right) + \beta_2 \hat{z}_t
\end{align*}
\]
Real Economy IV

Real Wage Gap:

- Introduced in January 2007
- Wage costs are above their equilibrium level, they have an inflationary effect
- The effect of a deviation of the current level of the average real wage from its equilibrium level, which in the long run rises at the same rate as equilibrium real output (non-accelerating inflation real output)

\[
\hat{WR}_t = \hat{WR}_{t-1} + \frac{W_t}{4} - \frac{\pi_t}{4} - \frac{\Delta \overline{WR}_t}{4} + \varepsilon_t^{WR}
\]
Real Economy V

Unemployment:

- Okun law
- Unemployment gap depends on its lag output gap.
Phillips Curves I

Price Inflation:

- Standard Phillips curve has been modified for a small open economy
- Blocks for various goods
- Import price effects
- Wage setters derive their nominal wage demand real consumer wage

- $x$ for fuel, food, or adjusted excl. fuel inflation
- Administered prices are exogenous in baseline
Phillips Curves II

\[ \pi^x_t = \gamma_1^x \left( \pi^M_{4t} + \Delta_4 \bar{z}^x_{t} \right) + \gamma_2^x \left( E \pi^4_{4t} + \Delta_4 \bar{z}^x_{t} - \Delta_4 \bar{z}_t \right) 
+ (1 - \gamma_1^x - \gamma_2^x) \pi^x_{t-1} + \gamma_3^x \hat{m}_c_t + \varepsilon^x_t \]

Wage Inflation:


\[ w_t = \delta_1 E w 4_t + (1 - \delta_1) w_{t-1} - \delta_2 \left( \hat{w}r_t - \delta_3 \hat{y}_t \right) + \varepsilon^w_t \]
**Expectations I**

**Price Inflation Expectations:**
- Expected inflation: a weighted combination of a backward-looking and a forward-looking component (the expected value of overall CPI inflation over the next four quarters)
- Overall CPI: an explicit link between changes in administered and energy prices and pressures on the rate of inflation for market prices

\[ E\pi_{4t} = \lambda_1 \pi_{t+1} + (1 - \lambda_1) \pi_{t-1} + \varepsilon_t^{E\pi_4} \]

**Wage Inflation Expectations:**

\[ Ew_{4t} = \lambda_2 w_{t+1} + (1 - \lambda_2) w_{t-1} + \varepsilon_t^{Ew_4} \]
Uncovered interest rate parity

Nominal Exchange Rate:

- UIP condition: arbitrage condition; international investors will equalize effective rates of return on investments in different currencies, allowing for any country-specific risk premiums
- foreign investor expecting a depreciation (appreciation) of the koruna will demand a higher (lower) return from Czech assets
- Moving average form

\[
S_t = \phi S_{t+1} + (1 - \phi) \left( S_{t-1} + 2 \left( \frac{E_t \pi}{4} - \frac{E_t \pi^f}{4} \right) + 2 \Delta \bar{z}_t \right) \\
+ \frac{i_t}{4} - \frac{i_t^f}{4} - \text{prem}_t + \varepsilon_t
\]
Reaction Function

Nominal Interest Rate:
- Forward-looking reaction function
- CPI inflation expected to be above the target rate: central bank push up the short-term
- Excess demand: the central bank increases short-term interest rate
- Long-term level for rates and some additional dynamic structure
- Interest rate inertia: interest rate smoothing

\[
\begin{align*}
i_t &= \psi i_{t-1} + (1 - \psi) \left( i_{t}^{neutral} + \Pi_t \right) + \varepsilon_t \\
i_{t}^{neutral} &= \bar{\Pi}_t + \pi_{4t+4} + \varepsilon_t \\
\Pi_t &= \kappa_1 \left( \pi_{4t+4} - \pi_{4t+4}^{target} \right) + \kappa_2 \hat{Y}_t
\end{align*}
\]
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Calibration vs. Estimation

- QPM is calibrated, partially estimated
- Problems in estimation:
  - Short data sample
  - Structural changes in economy
  - Changes of monetary policy regime
  - It is impossible to estimate some parameters: identification problems
Calibration of QPM

Parameters setup:
- Restrictions on parameters originating from economic theory
- Parameters are set to match the properties of data
- Responses to structural shocks

Parameters checks:
- Reactions to shocks
- Residuals
- In-sample simulations
- Curve-fitting estimates
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Price shock I

- Positive shock to the output gap
- Upward pressure on inflation
- Currency depreciation
- Central bank increases interest rate
- Cumulative effect on output is very close to zero: feature of linear models;
- Offsetting of excess supply to counteract the effects of shocks that create excess demand
Price shock II

- Interest rate
- Price inflation
- Wage inflation
- Exchange rate appreciation
- Real marginal costs gap
- Output gap
Aggregate demand shock I

- Positive shock to the output gap
- Upward pressure on inflation
- Currency depreciation
- Central bank increases interest rate
- Cumulative effect on output is very close to zero: feature of linear models;
- Offsetting of excess supply to counteract the effects of shocks that create excess demand
Aggregate demand shock II

- Interest rate
- Price inflation
- Wage inflation
- Exchange rate appreciation
- Real marginal costs gap
- Output gap
Exchange rate shock I

- Depreciation acts to increase aggregate demand, opening a positive output gap
Exchange rate shock II

- Interest rate
- Price inflation
- Wage inflation
- Exchange rate appreciation
- Real marginal costs gap
- Output gap
Inflation target change I

- Lower the target rate of inflation by one percentage point
- To achieve disinflation: raise the short rate
- Appreciation: Import prices fall
- The combined effect of the import price decline and the excess supply gap works to gradually pull down the rate of inflation
- Note: purely nominal shock, and since the model is super-neutral, there is no change to any real equilibrium in this shock, including the real exchange rate. The nominal exchange rate changes, of course, with the cumulative
- Cumulative effects on output and employment
- Sacrifice ratio: a cumulative loss of output vs. lower inflation by a percentage point
Inflation target change II
Residuals I

- Conflict between estimated parameters and calibrated
- The parameters have to be chosen so as to give reasonable model behavior
- Examined how well the model performs over the historical sample
- Identify systematic biases
Residuals II

*Adjusted ex. Fuels Inflation*

*Output Gap*

*Exchange Rate*

*Nominal IR*
In-Sample Simulations: CPI
In-Sample Simulations: Ex. rate
In-Sample Simulations: GDP
In-Sample Simulations

3-Month Interbank Rate

- 2003Q1
- 2003Q3
- 2004Q1
- 2004Q3
- 2005Q1
- 2005Q3
- 2006Q1
- 2006Q3
- 2007Q1
- 2007Q3
- 2008Q1

Graph showing the 3-Month Interbank Rate from 2003 to 2008.
Modeling tools

- Implementation in Matlab
- IRIS by Jaromír Beneš
Univariate filtering I

- Hodrick-Prescott filter: optimally extracts a trend which is stochastic but moves smoothly over time and is uncorrelated with the cyclical component.

- Mathematics of HP filter:
  - Decomposition: \( y_t = \tau_t + c_t \)
  - Solve:
    \[
    \min \sum_{t=1}^{T} (y_t - \tau_t)^2 + \lambda \sum_{t=2}^{T-1} [(\tau_{t+1} - \tau_t) - (\tau_t - \tau_{t-1})]^2
    \]
    \[\lambda = 100 \times (\text{number of periods in a year})^2\]

- Assumption that the trend is smooth is imposed by assuming that the sum of squares of the second differences of \( \tau_t \) is small.

- Sensitivity of the trend to short-term fluctuations is achieved by modifying a multiplier \( \lambda \).
Univariate filtering II

**Drawbacks:**

- One-time permanent shock, split growth rates present: Filter identifies non-existing shifts in the trend
- It pushes noise in data to Normal distribution
- Misleading predictive outcome: Analysis is purely historical and static
Univariate filtering III

- Trend:

![Graph showing trend analysis with HP filtering]
Univariate filtering IV

- Gap:
Kalman filter I

- Separate the cyclical component of a time series from raw data
- Can handle more series and exploit relations between them
- Kalman filter is a powerful tool for:
  - Estimation
  - Prediction
  - Smoothing

Kalman filter:
- Online estimation procedure
- States are estimated, when the new observations are coming in

Kalman smoother:
- Off-line estimation procedure
- The state estimation of is not only based on all previous observations, but also on all later observations
Kalman filter II

- $F$ is the state transition model
- $B$ is the control-input model
- $H$ is the observation model
- $w$ is the process noise
- $z$ is the measurement
- $v$ is the measurement error
- $u$ is the exogenous control
Kalman filter structure

Central bank \rightarrow Controls \rightarrow System \rightarrow System state \rightarrow Measuring device \rightarrow Measurement errors \rightarrow Kalman filter \rightarrow Optimal estimate of system state
Description of variables

- Measurement variables: $\Delta EU_{LGDP}, EU_{LGDPGAP}_EXPERT$
- State variables: $\Delta EU_{LGDP_EQ}, MU, EU_{LGDPGAP}$
- Exogenous-variables: $EU_{RMCIGAP}$
- Shocks: $\nu$’s
- Coefficients: $a_1, a_2, a_3$ and $\mu_{SS}$
- Variance: $\sigma_1, \sigma_2, \sigma_3, \sigma_4$
- Remark: In the following slides the filtering is actually smoothing
Description of model

- **Measurement equations:**

\[ \Delta EU\_LGDP = \Delta EU\_LGDP\_EQ + 4 \times (EU\_LGDP\_GAP - EU\_LGDP\_GAP\{\text{-1}\}) \]

\[ EU\_LGDP\_GAP = EU\_LGDP\_GAP\_EXPERT + \sigma_4 \times \nu_4 \]

- **State equations:**

\[ \Delta EU\_LGDP\_EQ = \mu + \sigma_1 \times \nu_1 \]

\[ \mu = (1 - a_3) \times \mu_{SS} + a_3 \times \mu\{\text{-1}\} + \sigma_3 \times \nu_3 \]

\[ EU\_LGDP\_GAP = a_1 \times EU\_LGDP\_GAP\{\text{-1}\} + a_2 \times EU\_RMCGAP\{\text{-1}\} + \sigma_2 \times \nu_2 \]
Filtering results: EU Eq. trajectories

KF filtering, EU EQ - log(levels)
Filtering results: EU Gap estimate


- LGDP-GAP-EU-new
- LGDP-GAP-EU-old
Filtering results: Removing volatility

KF filtering, EU EQ - q-o-q growth ann.

LGDP-EU
LGDP-EU-EQ
Appendix

Filtering results

Model setting: Changes in volatility of gap $\sigma_2$


- LGDP-GAP-EU-origin
- LGDP-GAP-EU-high
- LGDP-GAP-EU-low

I/96 I/97 I/98 I/99 I/00 I/01 I/02 I/03 I/04 I/05 I/06 I/07 I/08 I/09 I/10 I/11
Filtering domestic variables

- **First step:**
  - Decompose real variables: trend and cycle
  - Simple model for: Real interest rate, Real exchange rate, Exchange risk premium

- **Second step:**
  - Utilize measurement of inflation and wage growth
  - Fit simple backward-looking Phillips curves: relation between inflation and output gap
  - Fit IS curve: relation between output gap and gaps in real interest and exchange rate
  - Decompose: domestic output, real wage, unemployment
Filtering results: Domestic Eq. trajectory

KF filtering, CZ EQ - log(levels)

- LGDP-new
- LGDP-old
- LGDP-EQ-new
- LGDP-EQ-old
Filtering results: Domestic output gap


- LGDP-gap-new
- LGDP-gap-old
Description: Second step model

- **Measurement variables:** \( DOT\_LGDP, DOT\_UNR, PIE\_CORE, PIE\_W, DOT\_LWR, LWR\_GAP\_EXPERT, LGDP\_GAP\_EXPERT, UNR\_GAP\_EXPERT \)

- **State variables:** \( DOT\_LGDP\_EQ, MU, LGDP\_GAP, DOT\_UNR\_EQ, UNR\_GAP, PIE\_CORE\_S, PIE\_W\_S, DOT\_LWR\_EQ, LWR\_GAP \)

- **Exogenous variables:** \( RRC\_GAP, RR4\_GAP, EU\_RR4\_GAP, LZ\_GAP, EU\_LGDP\_GAP, PIE\_M\_XENERGY4, DOT\_LZ\_CORE\_EQ4, DOT\_LZ\_EQ4, E0\_CORE4, E0\_PIE\_W4, DOT\_LWR\_PRIOR, E0\_PIE4 \)

- **Shocks:** \( \nu_s \)

- **Variance:** \( \sigma_s \)
Model 1

- Measurement equations:

\[
\begin{align*}
\text{DOT\_LGDP} & = \text{DOT\_LGDP\_EQ} + 4 \times (\text{LGDP\_GAP} - \text{LGDP\_GAP}\{ -1 \}) \\
\text{DOT\_UNR} & = \text{DOT\_UNR\_EQ} - 4 \times (\text{UNR\_GAP} - \text{UNR\_GAP}\{ -1 \}) \\
\text{PIE\_CORE} & = \text{PIE\_CORE\_S} \\
\text{PIE\_W} & = \text{PIE\_W\_S} \\
\text{DOT\_LWR} & = \text{DOT\_LWR\_EQ} + 4 \times (\text{LWR\_GAP} - \text{LWR\_GAP}\{ -1 \}) \\
\text{LWR\_GAP} & = \text{LWR\_GAP\_EXPERT} + \text{std}_w3 \times \nu \text{LWR\_GAP\_EXPERT} \\
\text{LGDP\_GAP} & = \text{LGDP\_GAP\_EXPERT} + \text{std}_w1 \times \nu \text{LGDP\_GAP\_EXPERT} \\
\text{UNR\_GAP} & = \text{UNR\_GAP\_EXPERT} + \text{std}_w2 \times \nu \text{UNR\_GAP\_EXPERT}
\end{align*}
\]
Model II

State equations:

\[ \text{DOT} \_ \text{LGDP} \_ \text{EQ} = MU\{ -1 \} + a1 \ast \text{DOT} \_ \text{UNR} \_ \text{EQ} + \text{std} \_ \nu1 \ast \nu \_ \text{DOT} \_ \text{LGDP} \_ \text{EQ} \]
\[ \text{LGDP} \_ \text{GAP} = \text{LGDP} \_ \text{GAP} \_ \text{C}01 \ast \text{LGDP} \_ \text{GAP}\{ -1 \} - \text{RMCI} \_ \text{GAP} \_ \text{C}02 \ast (b2 \ast \text{RRC} \_ \text{GAP}\{ -1 \}) \]
\[ + b3 \ast \text{RR4} \_ \text{GAP}\{ -1 \} + b4 \ast \text{EU} \_ \text{RR4} \_ \text{GAP}\{ -1 \}) \]
\[ \text{LGDP} \_ \text{GAP} \_ \text{C}02 \ast \text{EU} \_ \text{LGDP} \_ \text{GAP} + \text{std} \_ \nu2 \ast \nu \_ \text{LGDP} \_ \text{GAP} \]
\[ \text{MU} = (1 - a3) \ast \text{MU} \_ \text{SS} + a3 \ast \text{MU}\{ -1 \} + \text{std} \_ \nu3 \ast \nu \_ \text{MU} \]
\[ \text{DOT} \_ \text{UNR} \_ \text{EQ} = \text{std} \_ \nu4 \ast \nu \_ \text{DOT} \_ \text{UNR} \_ \text{EQ} \]
\[ \text{UNR} \_ \text{GAP} = \text{UNR} \_ \text{GAP} \_ \text{C}01 \ast \text{UNR} \_ \text{GAP}\{ -1 \} \]
\[ + \text{UNR} \_ \text{GAP} \_ \text{C}02 \ast \text{LGDP} \_ \text{GAP} + \text{std} \_ \nu5 \ast \nu \_ \text{UNR} \_ \text{GAP} \]
\[ \text{PIE} \_ \text{CORE} \_ \text{S} = \text{PIE} \_ \text{CORE} \_ \text{C}01 \ast (\text{PIE} \_ \text{M} \_ \text{XENERGY4} + \text{DOT} \_ \text{LZ} \_ \text{CORE} \_ \text{EQ}4) \]
\[ + \text{PIE} \_ \text{CORE} \_ \text{C}02 \ast (\text{PIE} \_ \text{CORE} \_ \text{C}05 \ast \text{E0} \_ \text{CORE}4 \]
\[ + (1 - \text{PIE} \_ \text{CORE} \_ \text{C}05) \ast \text{E}0 \_ \text{PIE4} \]
\[ + (1 - \text{PIE} \_ \text{CORE} \_ \text{C}01 - \text{PIE} \_ \text{CORE} \_ \text{C}02) \ast \text{PIE} \_ \text{CORE} \_ \text{S}\{ -1 \} \]
\[ + \text{RMCI} \_ \text{GAP} \_ \text{C}01 \ast \text{PIE} \_ \text{CORE} \_ \text{C}03 \ast \text{LGDP} \_ \text{GAP} \]
\[ + \text{PIE} \_ \text{CORE} \_ \text{C}03 \ast \text{LWR} \_ \text{GAP} \]
\[ + \text{std} \_ \nu6 \ast \nu \_ \text{PIE} \_ \text{CORE} \]
\[ \text{PIE} \_ \text{W} \_ \text{S} = \text{PIE} \_ \text{W} \_ \text{C}01 \ast \text{E0} \_ \text{PIE} \_ \text{W}4 + (1 - \text{PIE} \_ \text{W} \_ \text{C}01) \ast \text{PIE} \_ \text{W} \_ \text{S}\{ -1 \} \]
\[ + \text{PIE} \_ \text{W} \_ \text{C}02 \ast (\text{LWR} \_ \text{GAP} - \text{PIE} \_ \text{W} \_ \text{C}03 \ast \text{LGDP} \_ \text{GAP}) + \text{std} \_ \nu7 \ast \nu \_ \text{PIE} \_ \text{W} \]
\[ \text{DOT} \_ \text{LWR} \_ \text{EQ} = \text{DOT} \_ \text{LGDP} \_ \text{EQ} + \text{DOT} \_ \text{LWR} \_ \text{PRIOR} + \text{std} \_ \nu8 \ast \nu \_ \text{DOT} \_ \text{LWR} \_ \text{EQ} \]
\[ \text{LWR} \_ \text{GAP} = f1 \ast \text{LWR} \_ \text{GAP}\{ -1 \} + \text{std} \_ \nu9 \ast \nu \_ \text{LWR} \_ \text{GAP} \]
Filtering results: Expert judgement


- UNR-GAP-orig
- UNR-GAP-old
- UNR-GAP-fix

I/96 I/97 I/98 I/99 I/00 I/01 I/02 I/03 I/04 I/05 I/06 I/07 I/08 I/09 I/10 I/11
Filtering results: Expert judgement


- LWR-GAP-orig
- LWR-GAP-old
- LWR-GAP-fix

I/96 I/97 I/98 I/99 I/00 I/01 I/02 I/03 I/04 I/05 I/06 I/07 I/08 I/09 I/10 I/11
Criticism of simple models: lack of reference to unemployment

J. Galí, F. Smets and R. Wouters (2011):
- Address this issue in an extended model
- Conclusion: Model-based output gap resembles conventional measures of the cyclical component of log GDP.
- Comparison of a variety of statistical detrending methods
- HP filter, band-pass filter, quadratic detrending, and the Congressional Budget Office’s measure
Advanced filtering
In search for future trends
List of Variables I

\( \hat{a} \) gap of the variable \( a \)
\( \bar{a} \) trend (equilibrium) value of the variable \( a \)
\( a^f \) variable \( a \) for the foreign country
\( \varepsilon^a \) residual in the equation for the variable \( a \)

mc real marginal costs
y real output
rw real wage
rmci real monetary condition index
r4 real 1Y interbank rate
r real 3M interbank rate
rc real rate of newly-issued bank loans
z real exchange rate
List of Variables II

\[ \pi_{4}^{\text{target}} \]
\[ \pi \]
\[ \pi_{4} \]
\[ w \]
\[ w_{4} \]
\[ \pi_{4}^{M} \]
\[ s \]
\[ \text{prem} \]
\[ i \]
\[ i_{\text{neutral}} \]
\[ \alpha, \beta, \gamma, \delta, \phi, \psi, \kappa, \lambda \]

inflation target (y-o-y)
price inflation (q-o-q)
price inflation (y-o-y)
wage inflation (q-o-q)
wage inflation (y-o-y)
imported inflation (y-o-y)
nominal exchange rate
risk premium
nominal short-term interest rate
policy neutral short-term interest rate
parameters
For Further Reading I


Jordi Galí and Frank Smets and Rafael Wouters

Peter K. Clark
For Further Reading II

- **Rudolph E. Kalman**
  A New Approach to Linear Filtering and Prediction Problems

- **Greg Welch and Gary Bishop**
  An introduction to the Kalman filter.

- **Harvey, Andrew C, 1985**
  Trends and Cycles in Macroeconomic Time Series
For Further Reading III

- Watson, Mark M, 1986
  Univariate Detrending Methods with Stochastic Trends
  *Journal of Monetary Economics, Vol. 18*, p. 49

- Athanasios Orphanides and Simon van Norden, 2002
  The Unreliability of Output-Gap Estimates in Real Time
  *The Review of Economics and Statistics, Vol. 84*, Num. 4
I'm writing a book of my guesses about future trends.

If it gets published then my guesses will seem more valid than other people's. I'll charge huge fees to share my "vision" with audiences.

Why would people pay huge fees for guesses?

Trend number one is that people aren't getting any smarter.